

# **The Productivity J-Curve: How Intangibles Complement General Purpose Technologies**

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based on work with:  
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*Technology-Enabled Disruption Conference  
Dallas Federal Reserve Bank  
May 22-23, 2019*

# The Modern Productivity Paradox

Our earlier work explored explanations for a paradox:

- Broad optimism about potential of AI and associated technologies

vs.

- Poor measured productivity performance in the data

Our proposed resolution: implementation lags

- Need to a) accumulate sufficient stocks of new capital and b) invent/install complementary innovations
- These processes can take decades

# Slowdowns and GPTs in History

“Engels’ pause” during early industrial revolution

- Wage growth stagnant even as output rose quickly

Only half of U.S. mfg establishments electrified in 1919

- 30 years after AC systems standardized

Computer capital in U.S. didn’t reach long-run level until late 1980s

- 25+ years after invention of integrated circuit
- Only half that level 10 years earlier

# Additional Potential Reason for the Paradox

This study explores another reason why productivity slowdowns might accompany new technologies:  
mismeasurement from GPT-related intangible capital

We theoretically characterize this using growth accounting

Empirically estimate effects from past GPTs (computer software and hardware) and, more speculatively, AI

# Intangibles and Productivity Measurement

How do intangibles affect productivity measurement?

$$Productivity = \frac{Output}{Input}$$

- Intangible capital would be an unmeasured input
  - This will cause productivity to be overstated
- But intangible capital investment also an output
  - This will cause productivity to be understated
- Net effect on productivity measurement depends on relative timing of input vs. output mismeasurement

# The J-Curve

We show actual minus true productivity growth ( $g_{TFP} - \widetilde{g}_{TFP}$ ) equals weighted difference between growth rates of intangible investment ( $g_I$ ) and installed intangible capital stock ( $g_K$ ):

$$g_{TFP} - \widetilde{g}_{TFP} = \sum \left( \frac{\lambda}{z} - 1 \right) \frac{zI}{Y} (g_I - g_K)$$

- Summation is over (possibly) multiple intangible types
- $\lambda/z$  is intangible's market value relative to purchase price
- $zI/Y$  is intangible investment as share of output
- $g_I - g_K$  is difference between investment and stock growth

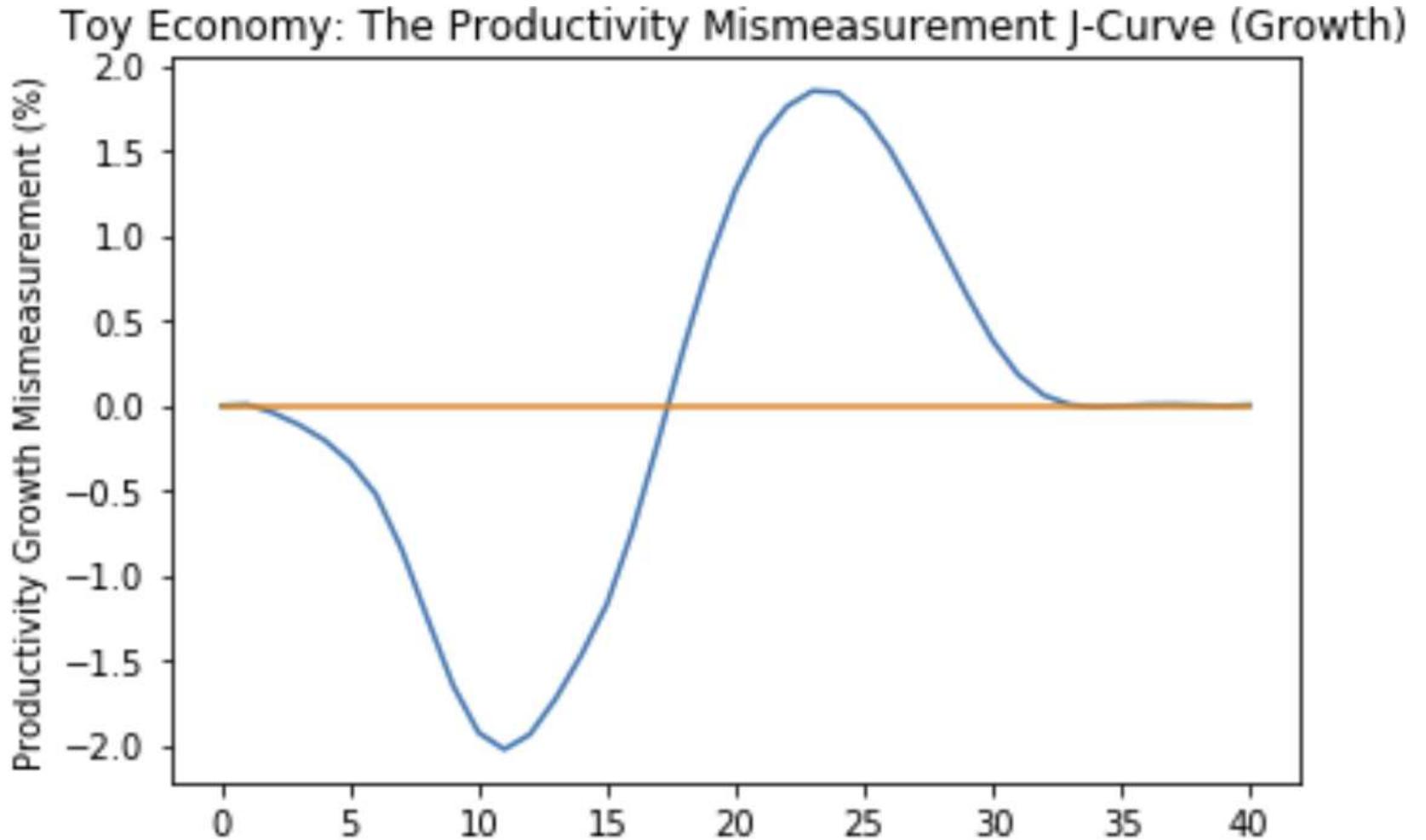
# The J-Curve

$$g_{TFP} - \widetilde{g_{TFP}} = \left( \frac{\lambda}{z} - 1 \right) \frac{zI}{Y} (g_I - g_K)$$

How might we expect mismeasurement to evolve (assuming  $\lambda > z$ )?

- Early in a GPT diffusion process,  $g_I$  likely larger than  $g_K$ , so true productivity growth higher than measured
- Later,  $g_I$  falls while  $g_K$  stays steady or rises; true productivity growth lower than measured
- Eventually, in steady state,  $g_I = g_K$ ; no mismeasurement (even as intangible investment continues)

# The J-Curve



# Empirical Strategy

Obviously, key element is the amount of intangible capital

How to measure intangibles?

- Suppose two types of  $K$ , tangible ( $j = 1$ ) and intangible ( $j = 2$ )
- Firm makes intangible investments that accompany tangible investments, so that  $K_2(t) = \mu K_1(t)$
- Firm's market value is then

$$V = \lambda_1 K_1 + \lambda_2 K_2 = \lambda_1 K_1 + \lambda_2 \mu K_1 = (\lambda_1 + \lambda_2 \mu) K_1$$

- Thus regression of firm market value on tangible capital gives insight into stock and shadow value of intangible capital

# Empirical Strategy

Measure  $\lambda/z$  using firm value regressions

For different types of capital with  $\lambda > z$ , use estimates to construct measure of  $g_{TFP} - \widetilde{g_{TFP}}$

Integrate to find implied difference in TFP levels

# Firm Value Regressions: R&D

Table 1: Market Value Regressions on R&D and SG&A Stocks

Market Value Regressions (1962-2017)	(1) Basic R&D	(2) Basic R&D and SG&A	(3) Industry-Year Fixed Effects: R&D	(4) Industry-Year Fixed Effects: R&D and SG&A	(5) Firm and Year Fixed Effects: R&D	(6) Firm and Year Fixed Effects: R&D and SG&A
Total Assets	1.016 (0.00179)	0.998 (0.00232)	1.015 (0.00853)	0.999 (0.0107)	1.013 (0.00725)	0.997 (0.0110)
R&D Stock	2.730 (0.105)	1.753 (0.0970)	2.841 (0.479)	1.953 (0.399)	2.161 (0.297)	1.509 (0.278)
SG&A Stock		1.755 (0.102)		1.657 (0.399)		1.453 (0.374)
Constant	656.8 (14.32)	458.7 (18.06)				
Firm-Year Observations	268,687	268,687	266,795	266,795	267,683	267,683
R-squared	0.987	0.988	0.989	0.989	0.993	0.993
Industry-Year FE	No	No	Yes	Yes	No	No
Firm and Year FE	No	No	No	No	Yes	Yes

Robust standard errors in parentheses

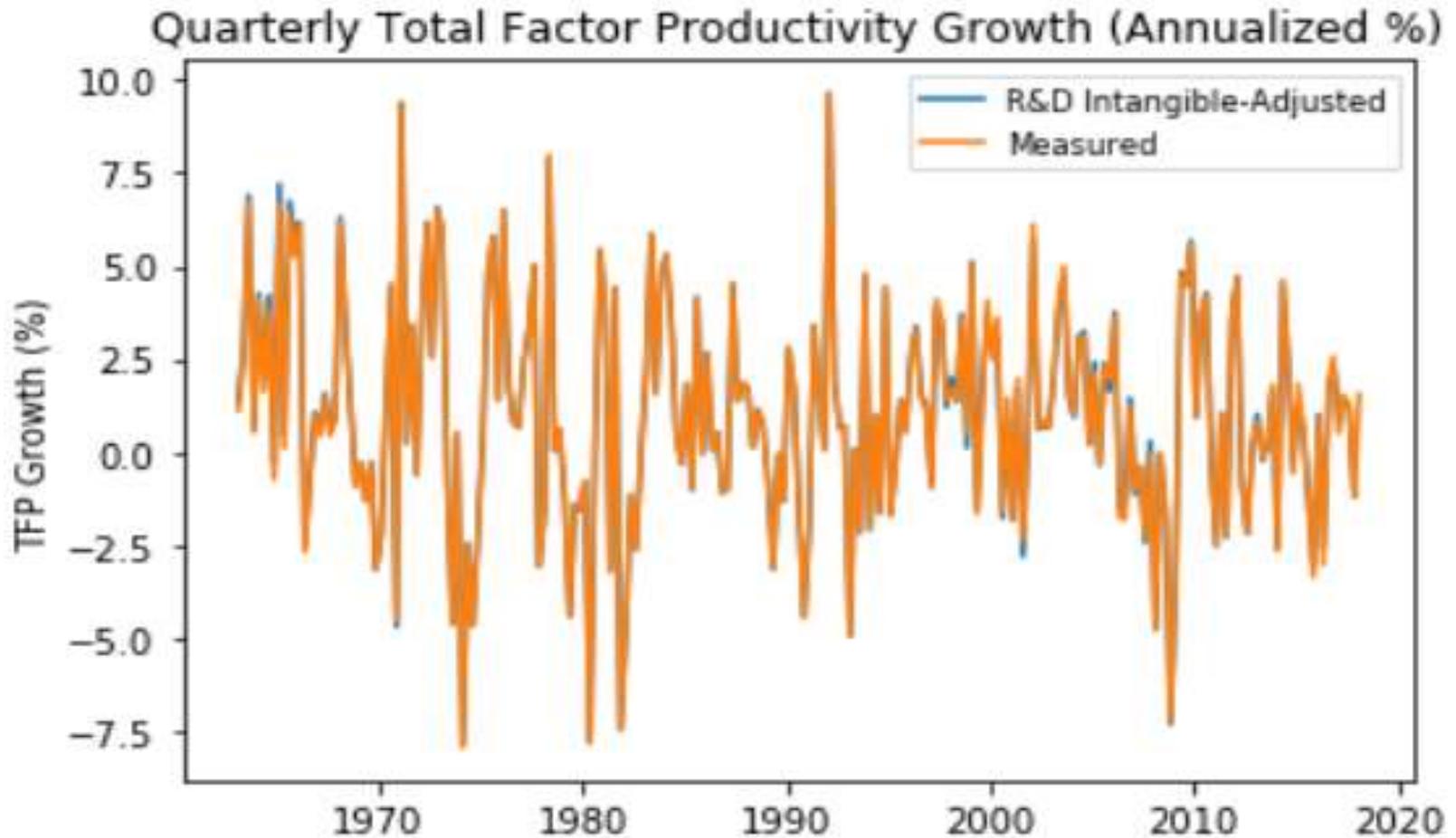
# Firm Value Regressions: R&D

Tangible “standard” capital appears to be valued dollar-for-dollar, both across companies and within companies over time

OTOH, \$1 of R&D appears to be associated with \$2 of shadow value, so perhaps \$1 dollar of intangibles per \$1 R&D

SG&A proxy for intangibles captures some of this, but also seems to be correlated with shadow value above \$1

# Measured and Adjusted TFP Growth: R&D



# Adjusted TFP: R&D

Why is mismeasurement so small if for every dollar of R&D there is an implied additional \$1 of intangible capital?

Because R&D investment rates have been stable for decades

Thus  $g_I \approx g_K$

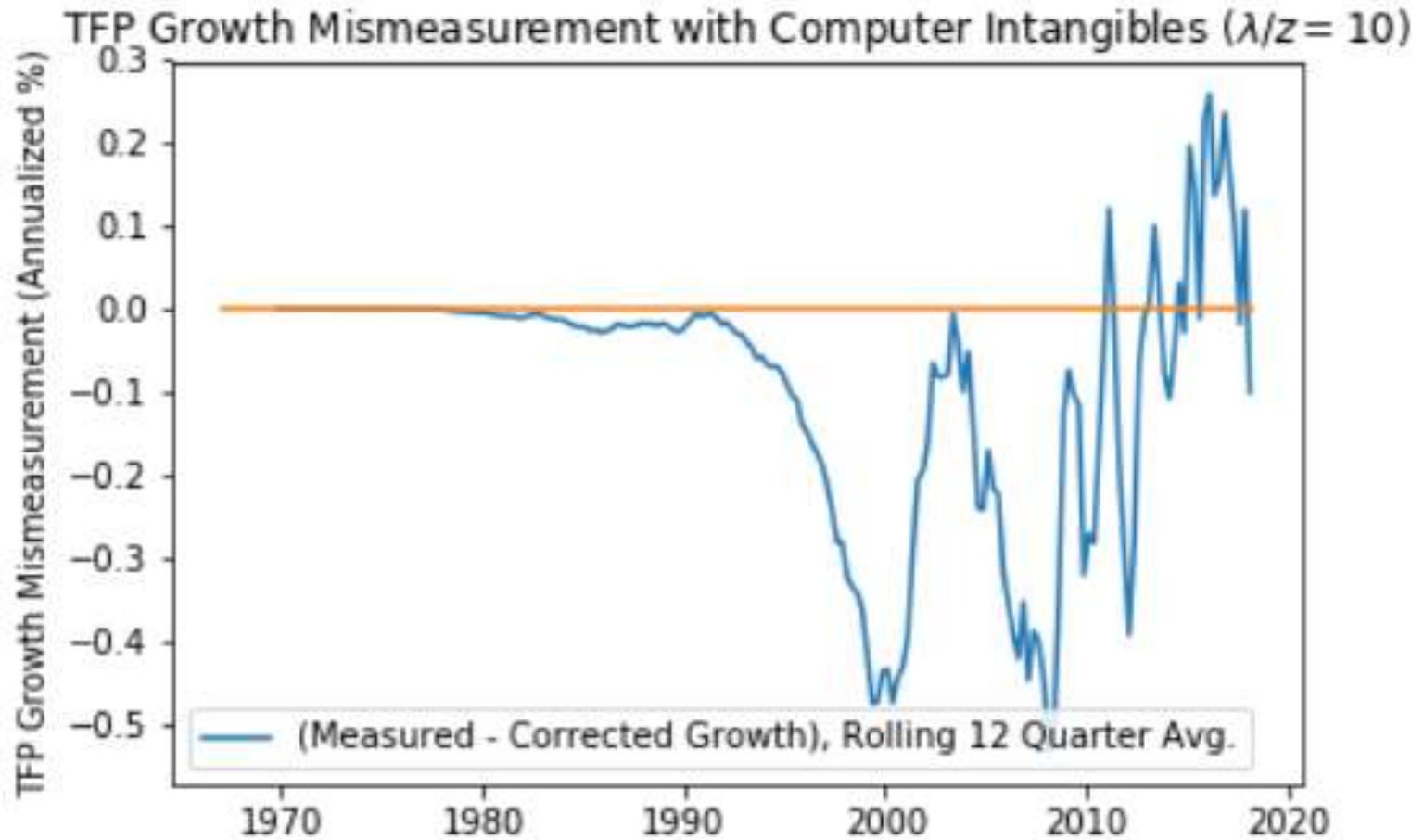
# Firm Values: Hardware and Software

We don't have firm-level IT capital data as we did for R&D

We instead proceed by computing implied mismeasurement for different values of  $\lambda/z$  based on the literature

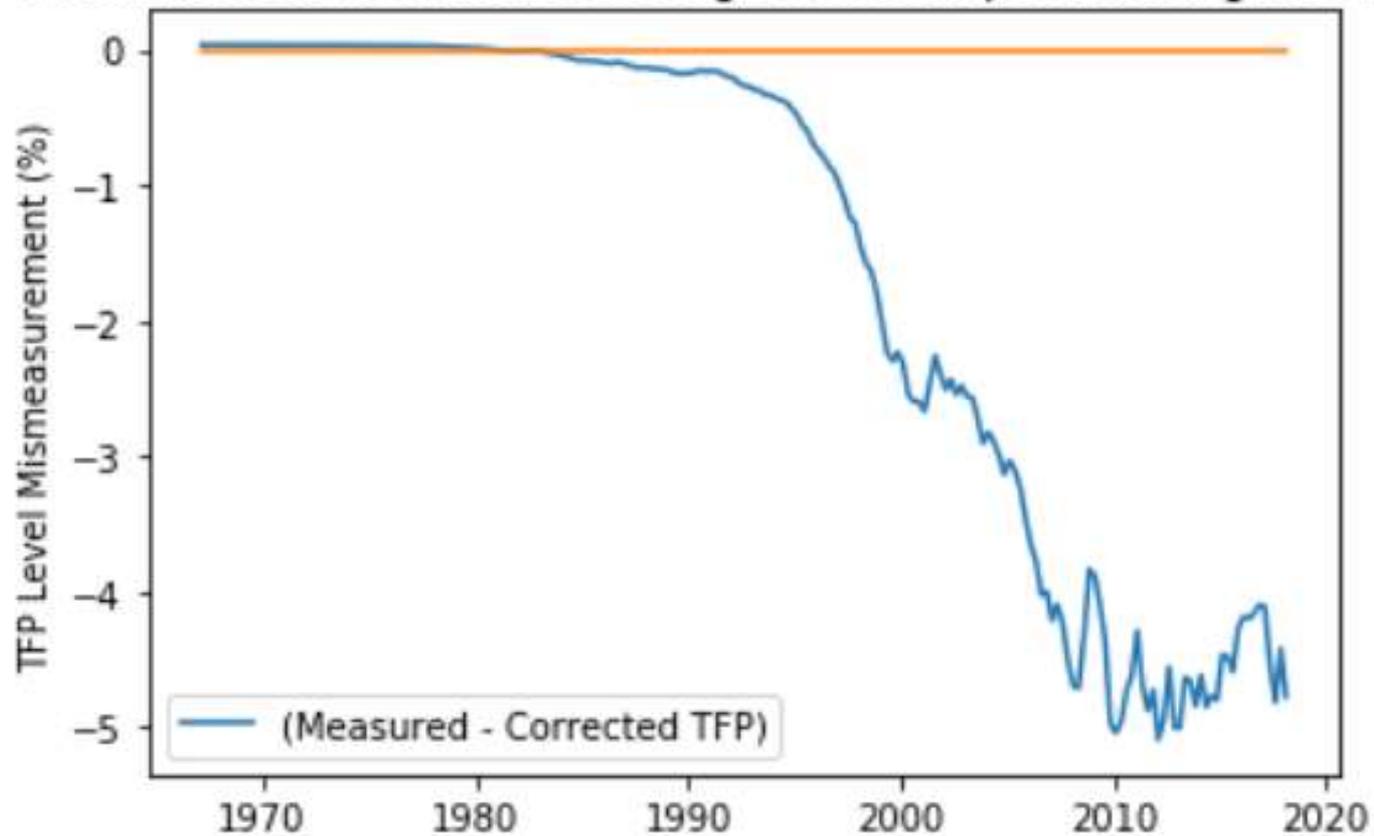
- Brynjolfsson, Hitt, and Yang (2002) estimate \$1 of computer hardware and software associated with about \$12 (s.e. = \$4) of market value
- We use  $\lambda/z$  of \$10; results change proportionately for alternative values of \$5, \$3, and \$2

# TFP Growth Mismeasurement by Year: IT Hardware



# TFP Accumulated Level Mismeasurement: IT Hardware

TFP Level Mismeasurement Percentage with Computer Intangibles ( $\lambda/z = 10$ )

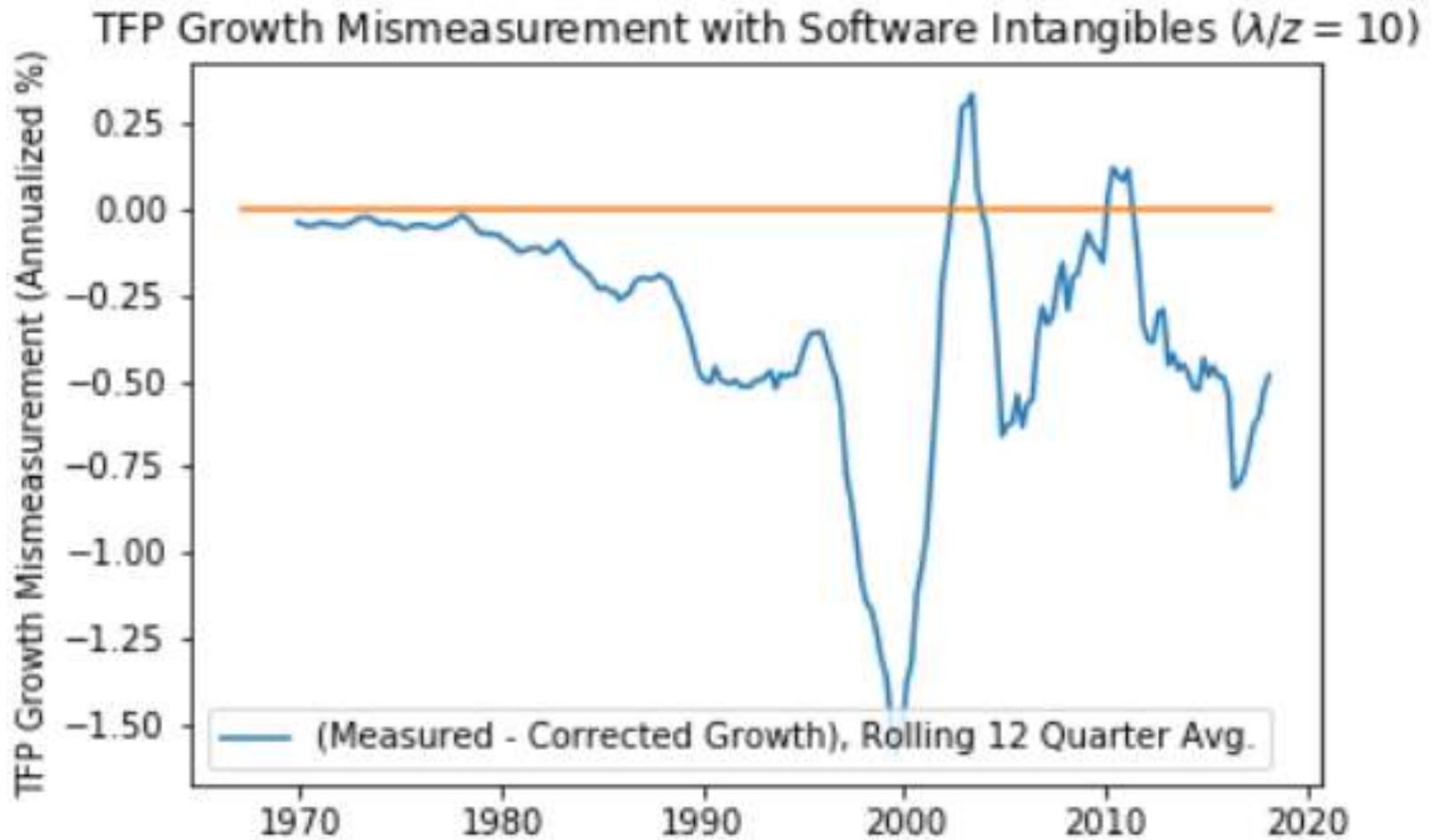


# Adjusted TFP: IT Hardware

Adjusted TFP level is 4.4% higher in 2016 than measured

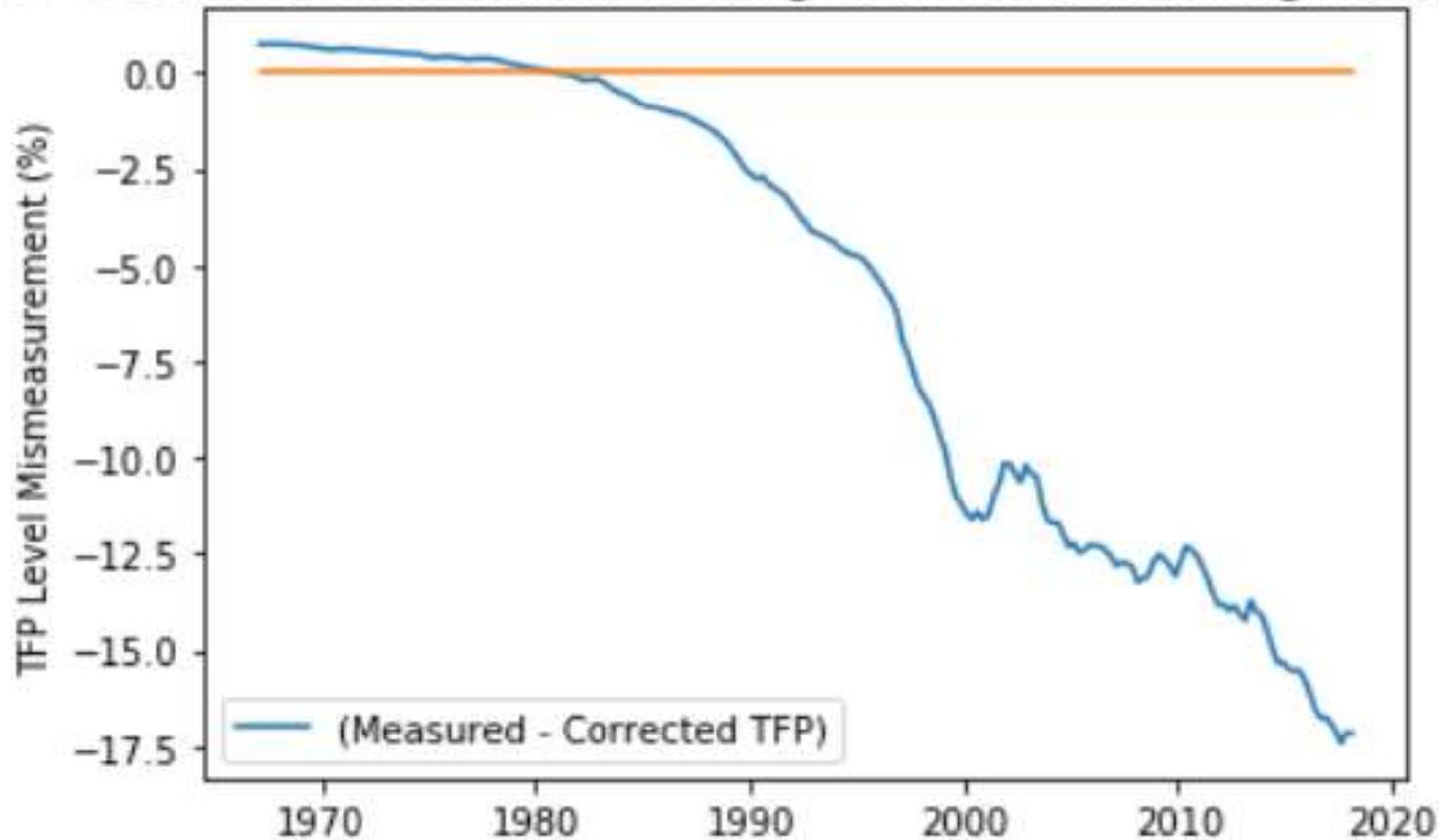
- Note this is the total growth measurement error accumulated over almost 50 years
- First half of *growth* J-curve has played out; hardware-related intangible accumulation has caused productivity growth overstatement (and brought levels back toward measured level) in past couple of years

# TFP Growth Mismeasurement by Year: IT Software



# TFP Accumulated Level Mismeasurement: IT Software

TFP Level Mismeasurement Percentage with Software Intangibles ( $\lambda/z = 10$ )



# Adjusted TFP: IT Software

Implied mismeasurement due to software-related intangibles is much larger than for intangibles related to R&D or hardware

Adjusted TFP level is 17% higher in 2016 than measured

First half of growth J-curve might be played out, but less clear than for hardware

# Does This Explain the Post-2004 Productivity Slowdown?

No; implied slowdown actually larger

A mismeasurement explanation for the slowdown doesn't require just mismeasurement; it requires a *change* in mismeasurement (in a particular direction and around 2004)

Period	Measured Annual TFP Growth (%)	Implied Annual TFP Growth (%)	Implied – Measured
1995-2004	1.63	2.53	0.90
2005-2017	0.40	0.85	0.45
Slowdown	1.23	1.68	0.45

# Are AI-Related Intangibles Causing Mismeasurement?

Still very early in AI adoption, but fast investment growth

Generous estimate of U.S. AI investments in 2018 is \$65-100B

If  $\lambda/z = \$10$ , that's \$650B to \$1T in missing output in the form of intangible investments (about 3-5% of GDP)

Likely an upper bound, plus it doesn't account for (still likely small) countervailing input effect of AI-related intangibles

- And note AI investments before past couple of years were probably too small to have had aggregate effects

# Conclusion

New technologies often require complementary intangible investments that can cause productivity mismeasurement

- First as missing output (productivity understatement)
- Later as missing input (productivity understatement)

This dynamic appears to have largely played out for R&D- and hardware-related intangibles

Still in play for software-related intangibles

AI-related intangibles might just now be creating enough mismeasurement to matter for aggregates