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The Effect of Central Bank Credibility on Forward Guidance in an Estimated New Keynesian Model*

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Abstract

This paper examines the effectiveness of forward guidance in an estimated New Keynesian model with imperfect central bank credibility. We estimate credibility for the U.S. Federal Reserve with Bayesian methods exploiting survey data on interest rate expectations from the Survey of Professional Forecasters (SPF). The results provide important takeaways: (1) The estimate of Federal Reserve credibility in terms of forward guidance announcements is relatively high, which indicates muted forward guidance effectiveness relative to the fully credible case. Hence, anticipation effects are attenuated and, accordingly, output and inflation do not respond as favorably to forward guidance announcements. (2) The so-called “forward guidance puzzle” is shown to arise, at least in part, from the unrealistically large responses of macroeconomic variables to forward guidance statements in structural models that do not incorporate imperfect credibility and heterogeneous expectations. (3) Imperfect monetary authority credibility provides a plausible explanation to the evidence of forecasting error predictability based on forecasting disagreement found in the SPF data. Thus, accounting for imperfect credibility is important to model the formation of expectations in the economy and to understand the transmission mechanism of forward guidance announcements.

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1. Introduction

Since the 2007 – 09 global financial crisis, it became apparent that central bank forward guidance is an essential monetary policy tool (as discussed in [BIS \(2019\)](#)). When short-term interest rates reached the zero lower bound (ZLB) in the aftermath of the global financial crisis, the U.S. Federal Reserve responded providing guidance on the future course of interest rates. The Federal Open Market Committee (FOMC) in its December 2008 statement already was framing its policy that way indicating that: “the Committee anticipates that weak economic conditions are likely to warrant exceptionally low levels of the federal funds rate for some time.”

This type of lower-for-longer policy at the ZLB has been recognized as an important part of the monetary policymakers toolkit and also shown in theory to have beneficial effects on the economy, as explained in the exploration of the New Keynesian model by [Woodford \(2003\)](#) and [Eggertsson and Woodford \(2003\)](#). Moreover, when interest rates are away from the ZLB, forward guidance can be effective as well providing clarification and transparency about future monetary policy. As explained by [Williams \(2013\)](#) and [Doehr and Martínez-García \(2015\)](#), greater clarity about the future policy path from forward guidance can help households and businesses make better investment decisions and boost the economy.

The effectiveness of forward guidance, in any event, rests on the perceived credibility of the central bank to follow through with its policy announcements. Standard macroeconomic models often consider the case of a fully credible monetary authority when investigating the impact that forward guidance can have on the economy. If the central bank is perceived as trustworthy, households and firms are likely to internalize the announcements about future policy in their decisions today (anticipation effects). If not, the effect on the economy from forward guidance is not as strong. Indeed, [Goodfriend and King \(2016\)](#) recognize this stating that “forecasts, and policy, should not be based solely on forecasts from a model that assumes full credibility in the stated policy path.” Thus, it is important to examine how the effectiveness of forward guidance depends on the credibility of the central bank.

This paper studies the effects of forward guidance with imperfect central bank credibility. A standard New Keynesian model augmented with standard macroeconomic persistence features (price stickiness, price indexation, habit formation, and interest rate inertia) is employed. The strategy by which the Federal Reserve has pursued forward guidance at the ZLB has evolved over time (as can be seen in Appendix C of [Caldara et al. \(2020\)](#)).¹ However,

¹A detailed summary of the timeline of policy actions and communications on forward guidance about the federal funds rate undertaken by the Federal Reserve in the aftermath of the 2007 – 09 global financial

following [Del Negro et al. \(2012\)](#) and [Laséen and Svensson \(2011\)](#), forward guidance is implemented flexibly by adding anticipated forward guidance shocks to the monetary policy rule. The model is then estimated using Bayesian methods with data on expectations—including interest rate expectations—from the Survey of Professional Forecasters (SPF).

Private agents that believe the central bank announcements about forward guidance are assumed to follow the full-information rational expectations (FIRE) typically employed in the literature. Those private agents who do not believe central bank announcements about forward guidance, instead, form forecasts based on a data-driven VAR(1) in output, inflation, and interest rates which effectively disregards all forward guidance announcements and only responds to the policy announced if and when it materializes.²

A key parameter in our analysis is $0 \leq \tau \leq 1$, which defines the weight assigned by private agents to the belief that the monetary authority forward guidance commitments are credible and would be honored. If $\tau = 1$, private agents believe the central bank to be perfectly credible and all announcements about forward guidance are honored. Thus, in that limiting case, aggregate expectations follow FIRE and we are back in the standard setup in the literature (e.g., [Del Negro et al. \(2012\)](#)). If $\tau \rightarrow 0$, in the limit private agents do not perceive the monetary authority to be credible and ignore forward guidance statements altogether. Aggregate expectations then do not contain forward guidance information and private agents do not anticipate and react to it.

The results from our estimated model show a number of takeaways. First, a distinctive contribution of our paper regards our use of Bayesian estimation procedures and the SPF dataset to tease out a measure of central bank credibility in regards to forward guidance from the empirical evidence available. We utilize expectations of the interest rate and other macro aggregates from the SPF to help identify forward guidance shocks. The estimate of the credibility parameter (i.e., τ) in terms of forward guidance announcements hovers around 0.8. Since the U.S. central bank is perceived as less than fully credible in its forward guidance announcements, there exists less immediate and overall anticipation effects on the economy from forward guidance than under the perfectly credible case. The impulse response

crisis can be found here: <https://www.federalreserve.gov/monetarypolicy/timeline-forward-guidance-about-the-federal-funds-rate.htm>.

²The structure of the model borrows from the axiomatic approach of [Branch and McGough \(2009\)](#) to represent aggregate expectations as a weighted sum of heterogenous private sector forecasts. The [Appendix](#) suggests that the mixture of forecasting strategies in the aggregate expectations can arise as an equilibrium from an evolutionary game-theoretic setup when incorporating central bank credibility and forward guidance into the model structure. This offers an alternative take on the formation of expectations which highlights the importance of non-cooperative games between the central bank and the private sector in our understanding of expectations.

functions and variance decomposition results in this paper show that the responses of output and inflation to forward guidance shocks do not respond as favorably relative to the scenario with a perfectly credible central bank.

Second, we also show that imperfect credibility is another important feature that contributes to the emergence of a so-called “forward guidance puzzle” in DSGE models. [Del Negro et al. \(2012\)](#) explain that the forward guidance puzzle arises because standard New Keynesian models produce unusually large responses to forward guidance news comparing model responses based on unconditional projections against projections conditional on setting the nominal interest rate near zero over an extended period of time (three years), while authors like [McKay et al. \(2016\)](#) argue that the anticipation effects on which forward guidance relies can be overstated in models where intertemporal consumption smoothing is largely unimpeded (under complete asset markets). We show that an economy that retains FIRE expectations and perfect credibility of the forward guidance announcements will also overstate the power of forward guidance. The credibility estimate that we obtain in our model, indeed, is not far away from the fully credible case but this still suffices to dampen considerably the power of forward guidance. Our evidence suggests that the attenuation that results from a forward guidance policy that is imperfectly credible weakens the quantitatively large forward guidance effects found by [Del Negro et al. \(2012\)](#).

Third, we provide supplementary evidence that our model capturing central bank credibility in terms of forward guidance aligns well with the data. In addition, the model of imperfect central bank credibility cross-validates well with certain features of the SPF data that have been left largely unaccounted for in the existing literature—in particular, with the predictability of forecasting errors based on forecasting disagreements. In both simulated data from our model and in the SPF data, we compare the empirical relationship between forecast errors and forecast disagreements with a standard regression. Our model of imperfect credibility can display comovements between the previously mentioned variables at different horizons that are broadly consistent with the comovements implied by the SPF dataset. In contrast, the perfectly credible central bank scenario cannot capture those features of the SPF data.

Finally, we examine additional alternative estimation strategies and different structural assumptions as further robustness checks. First, the main results do not substantially change if the model is estimated over our full sample (1981 : Q3–2018 : Q4), the non-ZLB subsample (1981 : Q3 – 2008 : Q4), or the Great Moderation period (1985 : Q1 – 2007 : Q3). In particular, the estimate of τ is high indicating a high level of trust in the central bank, but still below the fully credible case and similar to our baseline estimate for the full sample.

Second, our results are largely robust to a more agnostic prior belief about τ . The prior distribution in the baseline exercise was centered around a high degree of central bank credibility. When a less informative prior belief is assumed, our estimate of τ does not noticeably change in relation to the benchmark case (although it erodes somewhat). Third, the estimate of the monetary authority credibility parameter τ is similar to the benchmark results when we consider alternative forecasting models for those private agents who do not believe the central bank’s forward guidance statements. The estimate of τ does not noticeably change when habits in consumption or price indexation are turned off either. Fourth, the results are robust also if $t + 1$ expectations correspond to the one-period ahead forecasts in the SPF instead of corresponding to the nowcast as in our benchmark mapping between the data and the model.

In summary, by using Bayesian estimation procedures and SPF expectations data, we provide an estimate of the U.S. Federal Reserve credibility in relation to forward guidance. While we obtain a high level of central bank credibility from our evidence, the Federal Reserve is perceived as less than fully credible. Thus, our paper shows that accounting for imperfect credibility is important to model the formation of expectations in the economy and particularly so for the transmission mechanism of forward guidance announcements.

1.1. Contribution to the Literature

There exists a growing strand of the monetary policy literature focused on understanding the transmission mechanism through which forward guidance is thought to operate. This transmission channel relies on anticipation effects driven by a commitment to future policy that is made credibly. The evidence suggests that forward guidance moves expectations but only partially (Ferrero and Secchi (2009); Ferrero and Secchi (2010); Hubert (2014); Hubert (2015a); Hubert (2015b)). Mainstream theory also suggests that the anticipation effects are simply too strong within the standard class of New Keynesian equilibrium models (the so-called “forward guidance puzzle” of Del Negro et al. (2012)).³

Bundick and Smith (2020) find that the substantial effects of forward guidance found through the lens of the New Keynesian model by Del Negro et al. (2012) appear also in similarly constructed structural VAR models. Some authors like McKay et al. (2016) have argued, however, that capital market imperfections can be an important part of the story which can lead to overstating the macro effects of forward guidance. Other papers

³Related to this, Carlstrom et al. (2015) also show unusually large responses of the macroeconomic variables to interest rate pegs under a perfectly credible central bank.

have analyzed the expectations formation process of agents. [Gauss \(2015\)](#) and [Andrade et al. \(2019\)](#) show that heterogenous expectations in an economy can influence the power of forward guidance. [Cole \(2020a\)](#) and [Cole \(2020b\)](#) explain that the fully-informed rational expectations (FIRE) assumption can overstate the benefits of forward guidance relative to a more plausible adaptive learning rule used by agents subject to bounded rationality.

The effectiveness of forward guidance has also been analyzed via the communications channel. [Campbell et al. \(2019\)](#) find that FOMC forward guidance information has limited power at long horizons. [De Graeve et al. \(2014\)](#) argue that the effects of forward guidance on the economy can have more positive effects if its length is tied to the future condition of the economy (threshold-based forward guidance).⁴

The present paper is also related to prior research exploring the conduct of monetary policy when agents have imperfect information about the economy. Under an adaptive learning framework in which agents are uncertain about the true structure of the economy, [Eusepi and Preston \(2010\)](#) analyze different monetary policy communication strategies to ensure stable macroeconomic dynamics. [Honkapohja and Mitra \(2019\)](#) study central bank credibility in an adaptive learning framework when the monetary authority implements a price-level targeting policy.

[Ferrero and Secchi \(2009\)](#) and [Ferrero and Secchi \(2010\)](#) show that if the central bank communicates to the public its projections of the output gap and inflation, more desirable and stable outcomes can occur in the economy. [Orphanides and Williams \(2004\)](#), [Orphanides and Williams \(2007\)](#), [Gaspar et al. \(2006\)](#), and [Gaspar et al. \(2010\)](#) study central bank behavior when agents have imperfect information about the parameters in the central bank's policy rule function or optimal monetary policy with adaptive learning.

Our paper is closest to [Haberis et al. \(2014\)](#), [Goy et al. \(2018\)](#), and [Haberis et al. \(2019\)](#) which look at the role of monetary policy credibility.⁵ The former shows that forward guidance can help escape the liquidity trap when central bank credibility is endogenous. The latter paper explains that interest rate pegs can produce more muted responses of the macroeconomic variables if agents in their model are allowed to perceive the central bank as not credible.⁶

⁴[Campbell et al. \(2012\)](#) also examine Odyssean forward guidance (commitment to a future path of the policy rate) and Delphic forward guidance (publication of the central bank's own forecasts) in the U.S and find that the FOMC has achieved some success in communicating Odyssean forward guidance.

⁵Other papers related to ours include [Eggertsson and Woodford \(2003\)](#) who also discuss the importance of the management of expectations when the interest rate is constrained by the ZLB, and also [Kiley \(2016\)](#) and [Swanson \(2018\)](#) who explore forward guidance at the ZLB.

⁶[Nakata and Sunakawa \(2019\)](#) and [Dong and Young \(2019\)](#) examine time consistent policy in a model with forward guidance and credibility.

Altogether our paper adds to the literature along the following dimensions: (1) We introduce jointly the perceived credibility of the policy commitment and future policy news shocks, and relate both to the formation of heterogeneous private sector expectations. (2) We exploit SPF data on private sector expectations and Bayesian estimation techniques to analyze the effects of central bank credibility on the transmission of forward guidance shocks. Bayesian estimation procedures and survey data are employed to recover an estimate of central bank credibility in relation to forward guidance, which other studies have not estimated. To the best of our knowledge, none of the papers cited earlier explicitly estimates forward guidance and credibility jointly in a structural model as we do in our study. (3) Our estimation results show a high but imperfectly credible central bank in the U.S. This evidence implies that credibility has dampened the effects of forward guidance on the economy relative to the perfectly credible central bank case. We also show that a model with imperfect credibility and heterogeneous expectations is consistent with the forecastability of SPF forecasting errors based on forecasting disagreements amongst the individual SPF forecasters.

In short, we argue that both macro data and expectations data are better described with a model that incorporates heterogeneous expectations and deviations from FIRE behavior as a result of imperfect credibility on forward guidance which arises from policy commitments about the future path of the interest rate that can be reneged by the central bank (or limited commitment). Therefore, from our estimation, we conclude that the anticipation effects of forward guidance in the U.S. are attenuated—at least in part—because the central bank is perceived by private agents as unable to fully commit to honor the announced future path.

The remainder of the paper goes as follows: In [Section 2](#) we discuss our baseline model with heterogenous expectations and central bank credibility. In [Section 3](#) we introduce our Bayesian estimation approach which is based on an expectations-augmented linearized version of the general equilibrium model. In [Section 4](#) we present our main findings, while in [Section 5](#) we provide additional robustness checks on our key estimate of central bank credibility. In [Section 6](#) we conclude. We include in the [Appendix](#) an evolutionary game-theoretic motivation of our notion of central bank credibility and its connection to heterogenous expectations as well as all listed tables and figures.

2. Benchmark Model

We employ a standard New Keynesian model consistent with the workhorse framework laid out by [Woodford \(2003\)](#), [Giannoni and Woodford \(2004\)](#), [Milani \(2007\)](#), [Cúrdia et al. \(2015\)](#), and [Cole and Milani \(2017\)](#). The log-linear approximation that we bring to the data is derived from the optimizing behavior of households and firms. Our variant of the model includes four conventional sources of macroeconomic persistence—habit formation in consumption, price stickiness, price indexation, and interest rate inertia—to capture the dynamics of the macroeconomic data.

The model is completed with a [Taylor \(1993\)](#) interest rate feedback rule with inertia which describes the response of monetary policy to domestic economic conditions. We augment the standard monetary policy rule in one important dimension by explicitly distinguishing between unanticipated (surprises) and anticipated (forward guidance) news shocks to monetary policy. This distinction allows us to investigate the central bank’s commitment to a future path of the nominal policy rate (forward guidance) through the lens of a general equilibrium New Keynesian model. We describe the monetary policy rule in greater detail in [Subsection 2.2](#).

We, however, depart from the full-information rational expectations (FIRE), homogeneous-beliefs paradigm embedded in the workhorse New Keynesian model.⁷ Private agents are modeled as heterogeneous-beliefs households-firms that assign odds to whether the central bank will honor its forward guidance commitments or not. If the central bank’s commitments are deemed credible, then rational expectations forecasts are used with full recognition of the credibility odds. If they are deemed not credible, then expectations are formed on the basis of standard VAR techniques used to fit the data. VAR techniques are fairly easy to implement, yet are immune to attempts to “manage expectations” on the part of the central bank through forward guidance announcements that can be renege and never materialize.⁸

⁷Note that, as argued by [Park \(2018\)](#), monetary authorities typically employ macroeconomic models with rational expectations to forecast future economic activity as well as the future path of inflation and the policy rate—that is, models that do not incorporate the sort of heterogeneity that we capture here.

⁸A VAR model can be seen as a reduced-form representation of the solution to the rational expectations model without forward guidance announcements ([Martínez-García \(2018\)](#)), but it is more flexible to use a VAR for forecasting than to use that structural specification itself. This flexibility allows private agents to be agnostic about the policy rule (not just the commitments about the future path) and to form their expectations solely on the basis of the observed macro outcomes and irrespective of how other agents choose to form their expectations.

2.1. Main Structural Relationships

As in [Cúrdia et al. \(2015\)](#), the workhorse New Keynesian model can be described by the following pair of log-linearized equations:

$$\tilde{x}_t = \mathbb{E}_t \tilde{x}_{t+1} - (1 - \beta\eta)(1 - \eta)(i_t - \mathbb{E}_t \pi_{t+1} - r_t^n), \quad (1)$$

$$\tilde{\pi}_t = \beta \mathbb{E}_t \tilde{\pi}_{t+1} + \xi_p (\omega x_t + ((1 - \beta\eta)(1 - \eta))^{-1} \tilde{x}_t) + \mu_t, \quad (2)$$

where

$$\tilde{y}_t \equiv y_t - \eta y_{t-1} - \beta \eta \mathbb{E}_t (y_{t+1} - \eta y_t), \quad (3)$$

$$\tilde{y}_t^n \equiv y_t^n - \eta y_{t-1}^n - \beta \eta \mathbb{E}_t (y_{t+1}^n - \eta y_t^n), \quad (4)$$

$$\tilde{x}_t \equiv \tilde{y}_t - \tilde{y}_t^n = x_t - \eta x_{t-1} - \beta \eta \mathbb{E}_t (x_{t+1} - \eta x_t), \quad (5)$$

$$\tilde{\pi}_t \equiv \pi_t - \iota_p \pi_{t-1}. \quad (6)$$

Here, the one-period nominal interest rate (i_t) is the policy rate, inflation (π_t) is the first-difference on the consumption price level in logs, and the output gap (x_t) is defined as $x_t \equiv y_t - y_t^n$, i.e., as the log-deviation of actual output (y_t) from its potential level absent all nominal rigidities (y_t^n).

Equation (1), often referred to as the dynamic Investment-Savings (IS) equation, describes the aggregate demand of the economy arising from the optimal decisions (the intertemporal Euler equation) of households. Equation (1) together with (3) – (5) implies that the current output gap (x_t) depends on expected one-period and two-period ahead output gaps, the lagged output gap, the current nominal interest rate (i_t), the expected one-period ahead inflation rate ($\mathbb{E}_t(\pi_{t+1})$), and the natural rate (r_t^n) which is the real rate of interest that would prevail absent all nominal rigidities. Here, the intertemporal rate of substitution is set to one. There exists habit formation in consumption given by the parameter $0 \leq \eta \leq 1$, and households' intertemporal discount rate is given by the parameter $0 < \beta < 1$.

Equation (2) denotes the New Keynesian Phillips Curve (NKPC) and follows from the optimizing decision of firms. These firms are owned by the households and are operated in a monopolistically competitive environment with [Calvo \(1983\)](#) staggered price-setting behavior and [Yun \(1996\)](#) price indexation, similar to [Christiano et al. \(2005\)](#). Consequently, equation (2) shows that inflation (π_t) depends on lagged inflation, the expected one-period ahead inflation ($\mathbb{E}_t(\pi_{t+1})$), the current output gap (x_t), the lagged output gap, the expected one-period ahead output gap, and a cost-push shock (μ_t).

A fraction of firms given by the parameter $0 \leq \theta \leq 1$ are assumed to be unable to adjust their prices every period, while the remaining fraction $(1 - \theta)$ of firms can. The non-reoptimizing firms index their prices to past inflation with the degree of indexation determined by the parameter $0 \leq \iota_p \leq 1$. Furthermore, the parameter $\omega > 0$ is the inverse of the Frisch elasticity of labor supply, while the composite coefficient ξ_p is defined as $\frac{(1-\theta\beta)(1-\theta)}{\theta}$ with β being the household's intertemporal discount factor and θ the constant fraction of non-reoptimizing firms per period.

We use (5) to re-express the system of equations given by (1) – (2) to describe the dynamics of the economy in terms of actual and potential output as follows:

$$\tilde{y}_t = \mathbb{E}_t(\tilde{y}_{t+1}) - (1 - \beta\eta)(1 - \eta)(i_t - \mathbb{E}_t\pi_{t+1} - r_t^n) - \mathbb{E}_t(\Delta\tilde{y}_{t+1}^n), \quad (7)$$

$$\begin{aligned} \tilde{\pi}_t &= \xi_p(\omega y_t + ((1 - \beta\eta)(1 - \eta))^{-1}\tilde{y}_t) + \beta\mathbb{E}_t\tilde{\pi}_{t+1} + \mu_t \\ &\quad - \xi_p(\omega y_t^n + ((1 - \beta\eta)(1 - \eta))^{-1}\tilde{y}_t^n). \end{aligned} \quad (8)$$

Based on the output potential transformation in (4), we can further re-write the system of equations in (1) – (2) to obtain that:

$$\begin{aligned} \tilde{y}_t &= \mathbb{E}_t(\tilde{y}_{t+1}) - (1 - \beta\eta)(1 - \eta)(i_t - \mathbb{E}_t\pi_{t+1} - r_t^n) \\ &\quad - (\eta y_{t-1}^n - (1 + \eta + \beta\eta^2)y_t^n + (1 + \beta\eta + \beta\eta^2)\mathbb{E}_t(y_{t+1}^n) - \beta\eta\mathbb{E}_t(y_{t+2}^n)), \end{aligned} \quad (9)$$

$$\begin{aligned} \tilde{\pi}_t &= \xi_p(\omega y_t + ((1 - \beta\eta)(1 - \eta))^{-1}\tilde{y}_t) + \beta\mathbb{E}_t\tilde{\pi}_{t+1} + \mu_t \\ &\quad - \xi_p \left(\begin{array}{l} -((1 - \beta\eta)(1 - \eta))^{-1}\eta y_{t-1}^n + (\omega + ((1 - \beta\eta)(1 - \eta))^{-1}(1 + \beta\eta^2))y_t^n \\ -((1 - \beta\eta)(1 - \eta))^{-1}\beta\eta\mathbb{E}_t(y_{t+1}^n) \end{array} \right), \end{aligned} \quad (10)$$

with the same structural relationships as the system of equations given by (7) – (8). This showcases that the dynamic IS and NKPC equations can be expressed in terms of three observable macro variables: output (y_t), inflation (π_t), and the policy rate (i_t), i.e., in terms of the three-variable vector $Y_t = [y_t, \pi_t, i_t]'$. Moreover, these equations also show that cost-push shocks (μ_t) as well as exogenously-driven shifts in the output potential (y_t^n) and the natural rate of interest (r_t^n) drive the dynamics of output (y_t) and inflation (π_t).

Frictionless Allocation. The potential output allocation (y_t^n) and the natural real rate (r_t^n) are important constructs in our analysis and represent the levels of output and of the real interest rate that would prevail absent all nominal rigidities. In that counterfactual

scenario, output potential (y_t^n) evolves according to the following equation:

$$\begin{aligned} \omega y_t^n + \frac{1}{(1-\beta\eta)(1-\eta)} (y_t^n - \eta y_{t-1}^n) - \frac{\beta\eta}{(1-\beta\eta)(1-\eta)} (\mathbb{E}_t (y_{t+1}^n) - \eta y_t^n) \\ = \frac{\eta}{(1-\beta\eta)(1-\eta)} (\beta \mathbb{E}_t (\gamma_{t+1}) - \gamma_t). \end{aligned} \quad (11)$$

The previous equation follows from [Cúrdia et al. \(2015\)](#). Equation (11) implies that output potential is a linear combination of current, lagged, and future expected values of output potential as well as current and future expected values of exogenous productivity growth, $\gamma_t \equiv \Delta \ln(A_t)$ where A_t denotes total factor productivity (TFP). Given the efficient allocation of the output potential (y_t^n) in (11), the household's intertemporal Euler equation implies that the natural rate of interest (r_t^n) can be expressed as:

$$r_t^n = \mathbb{E}_t (\gamma_{t+1}) - \omega \mathbb{E}_t (\Delta y_{t+1}^n). \quad (12)$$

Equations (11) and (12) highlight the close connection between output potential and the natural rate of interest both of which respond to a common shock—the exogenous shock to productivity growth (γ_t).

Here, we observe that the natural rate of interest depends: (a) positively on the forecastable components of next period's exogenous productivity growth (γ_t), and (b) negatively on the forecastable component of next period's growth rate of output potential (Δy_{t+1}^n) which itself depends on the exogenous productivity growth (γ_t) through equation (11). Intuitively, point (b) captures the negative effect on the real interest rate of a higher expected growth rate of marginal utility which, under standard market clearing conditions, directly influences potential hours worked and in turn potential output as well.

Exogenous (Non-Monetary) Shock Processes. The exogenous shock to productivity growth (γ_t) and the cost-push shock (μ_t) are assumed to follow standard AR(1) processes:

$$\gamma_t = \rho_\gamma \gamma_{t-1} + \varepsilon_t^\gamma, \quad (13)$$

$$\mu_t = \rho_\mu \mu_{t-1} + \varepsilon_t^\mu, \quad (14)$$

where $\varepsilon_t^\gamma \overset{iid}{\sim} N(0, \sigma_\gamma^2)$ and $\varepsilon_t^\mu \overset{iid}{\sim} N(0, \sigma_\mu^2)$.⁹ The persistence of the productivity growth and cost-push shocks is given by the parameters $0 < \rho_\gamma < 1$ and $0 < \rho_\mu < 1$, respectively. Similarly, the volatility of the productivity growth and cost-push shocks is given by $\sigma_\gamma^2 > 0$

⁹In regards to equation (13), we have also considered a specification with a constant term. The results were largely robust and did not qualitatively change the main conclusions of this paper.

and $\sigma_\mu^2 > 0$, respectively. We do not consider spillovers between productivity growth and cost-push shocks and assume that their respective innovations are uncorrelated at all leads and lags.

2.2. Monetary Policy

The monetary policymaker relies on the short-term nominal interest rate (i_t) as its policy instrument. A [Taylor \(1993\)](#)-type monetary policy rule is generally viewed as a simple and practical guide for the conduct of monetary policy in the U.S.¹⁰ Henceforth, we assume that the central bank follows a variant of the [Taylor \(1993\)](#) rule whereby the nominal interest rate responds to inflation deviations from its zero-inflation target (π_t) and possibly also to fluctuations in the output gap ($x_t \equiv (y_t - y_t^n)$), i.e.,

$$i_t = \rho i_{t-1} + (1 - \rho) (\chi_\pi \pi_t + \chi_x (y_t - y_t^n)) + \varepsilon_t^{MP}. \quad (15)$$

This policy rule ensures the determinacy of the equilibrium whenever the policy parameters satisfy the Taylor principle, that is, whenever $\chi_\pi > 1$ and $\chi_x \geq 0$. The rule also includes lagged interest rates with a smoothing parameter given by $0 \leq \rho < 1$ and an unanticipated monetary policy shock (ε_t^{MP}).

We recognize that the strategy by which the Federal Reserve has pursued forward guidance has evolved over time, so we introduce time-contingent forward guidance in the [Taylor \(1993\)](#) rule flexibly in the form of anticipated monetary policy shocks (news) following the approach of [Laséen and Svensson \(2011\)](#) and [Del Negro et al. \(2012\)](#). This approach has more recently been used in related work by [Cole \(2020a\)](#) and [Cole \(2020b\)](#). Specifically, the monetary policy rule in (15) is augmented as follows:

$$i_t = \rho i_{t-1} + (1 - \rho) [\chi_\pi \pi_t + \chi_x (y_t - y_t^n)] + \varepsilon_t^{MP} + \sum_{l=1}^L \varepsilon_{l,t-l}^{FG}, \quad (16)$$

where the unanticipated (surprise) monetary policy shocks (ε_t^{MP}) are combined with forward guidance (news) shocks ($\varepsilon_{l,t-l}^{FG}$ for all $l = 1, \dots, L$).¹¹ The length of the forward guidance horizon provided by the news shocks is defined by the horizon $1 \leq L < +\infty$ implying that

¹⁰A [Taylor \(1993\)](#)-type monetary policy rule tends to result in little loss of performance relative to an optimal discretionary rule as noted, e.g., by [Dennis \(2004\)](#). An alternative specification would be to set monetary policy trade-offs in terms of the real interest rate in deviations from the natural rate instead of tying it to a specific policy instrument (the nominal short-term interest rate) as in [Martínez-García \(2020\)](#). We leave all these considerations for future research.

¹¹[Schmitt-Grohé and Uribe \(2012\)](#) utilize anticipated shocks and describe them as “news”. However, they do not explicitly study forward guidance via monetary policy news shocks and its economic effects.

there is a finite number of L forward guidance shocks in the summation term in equation (16).

Monetary policy surprises and forward guidance shocks are assumed to be purely transitory or *i.i.d.*, i.e.,

$$\varepsilon_t^{MP} \stackrel{iid}{\sim} N(0, \sigma_{MP}^2), \quad (17)$$

$$\varepsilon_{l,t-l}^{FG} \stackrel{iid}{\sim} N(0, \sigma_l^{2,FG}), \quad \forall l = 1, \dots, L, \text{ and } 1 \leq L < +\infty. \quad (18)$$

Each $\varepsilon_{l,t-l}^{FG}$ in equation (16) represents anticipated or news shocks that private agents know about in period $t-l$ but do not affect the interest rate until l periods later, that is, until period t . The volatility of the unanticipated and anticipated monetary policy shocks is given by $\sigma_{MP}^2 > 0$ and $\sigma_l^{2,FG} > 0$ for all $l = 1, \dots, L$, respectively. The innovations of anticipated and unanticipated monetary policy shocks are uncorrelated with each other and with the cost-push shock and productivity growth shock innovations at all leads and lags.

Following [Laséen and Svensson \(2011\)](#) and [Del Negro et al. \(2012\)](#), the following recursive representation is added to the model's system of equations to describe the news shocks:¹²

$$v_{1,t} = v_{2,t-1} + \varepsilon_{1,t}^{FG}, \quad (19)$$

$$v_{2,t} = v_{3,t-1} + \varepsilon_{2,t}^{FG}, \quad (20)$$

$$\vdots$$

$$v_{L,t} = \varepsilon_{L,t}^{FG}. \quad (21)$$

Each component of the vector $v_t = [v_{1,t}, v_{2,t}, \dots, v_{L,t}]'$ represents all past and present central bank announcements to change the interest rate 1, 2, \dots , L periods later that private agents know in period t . In addition, we define $\psi_t = [\varepsilon_{1,t}^{FG}, \varepsilon_{2,t}^{FG}, \dots, \varepsilon_{L,t}^{FG}]'$ as the vector containing all current-period forward guidance shocks known today that affect the monetary policy rule 1, 2, \dots , L periods later. Equations (19) – (21) can be simplified to show that $v_{1,t-1}$ corresponds to the last term in equation (16), i.e., the summation of all anticipated monetary policy shocks realized at time t , $v_{1,t-1} = \sum_{l=1}^L \varepsilon_{l,t-l}^{FG}$.

¹²[Laséen and Svensson \(2011\)](#) argue that standard solution techniques apply when forward guidance is modeled as described here rather than as a peg on the future path of the policy rate. Moreover, this implementation also helps us avoid the indeterminacy issues which can arise when modeling central bank forward guidance as pegging the future path of interest rates to a certain value (see, e.g., [Honkapohja and Mitra \(2005\)](#) and [Woodford \(2005\)](#)). Indeed, the method used here based on anticipated monetary policy shocks (news) alleviates this concern.

Accordingly, the policy rule in (16) can be re-expressed more compactly as:

$$i_t = \rho i_{t-1} + (1 - \rho) [\chi_\pi \pi_t + \chi_x (y_t - y_t^n)] + \varepsilon_t^{MP} + v_{1,t-1}. \quad (22)$$

The method of using equations (22) together with (17) – (21) provides a tractable way to incorporate anticipated monetary policy (forward guidance) news shocks as well as conventional unanticipated (surprise) monetary policy shocks into the monetary policy rule. Forward guidance shocks, therefore, can be interpreted as the means by which the central bank communicates (announces) the time-contingent path of future policy rates.

We choose to model forward guidance shocks in this way for a number of conceptual and practical reasons. First, we model forward guidance here following in the footsteps of the prior literature starting with [Laséen and Svensson \(2011\)](#) and [Del Negro et al. \(2012\)](#). That provides a degree of comparability. Second, the Federal Reserve’s forward guidance strategy has evolved. In the aftermath of the 2007-09 global financial crisis, the U.S. central bank forward guidance communication was “Odyssean” in nature but moved from calendar-based into state-contingent commitments over time. By 2012, the Fed also started to issue its own fed funds rate projections on top of the macro projections already being released since 2008 through the Fed’s Summary of Economic Projections (SEP) (“Delphic” forward guidance).¹³ All of these types of forward guidance share the same theme of communicating about the future course of policy. And equation (16) captures this feature in a reduced- but flexible form. We use this reduced-form representation as a simple and flexible way to encompass the different approaches of forward guidance followed by the Federal Reserve.

Expectations Augmented Vector of Observable Variables. The state equations that describe the dynamics of the economy in (9) – (10), together with (3) – (4) and (6), pin down the solution to the vector of three observable macro variables given by $Y_t = [y_t, \pi_t, i_t]'$ which includes actual output (y_t), inflation (π_t), and the policy rate (i_t). However, with monetary policy shocks split into unanticipated (surprise) and anticipated (news) shocks, the vector of observable variables Y_t lacks fundamentalness in the sense of [Hansen and Sargent \(1980\)](#) and [Martínez-García \(2018\)](#). In other words, these three observable macro variables do not contain enough information to pin down the vector of unobserved structural shocks $\varepsilon_t = \left(\gamma_t, \mu_t, \varepsilon_t^{MP}, \{\varepsilon_{l,t-l}^{FG}\}_{l=1}^L \right)'$. Without additional observable variables, we can only recover residuals that are linear combinations of the underlying structural shocks.

¹³[Campbell et al. \(2012\)](#) explain that Odyssean forward guidance is defined as policy guidance that publicly commits the central bank to a future course of action while Delphic forward guidance hinges on the publication of the central bank’s own forecasts to communicate future policy.

Given the monetary policy rule in equation (16), we can show that the expected future path of the policy rate at time t can be written as follows:¹⁴

$$\mathbb{E}_t(i_{t+s}) = \begin{cases} \rho i_{t-1} + (1 - \rho) [\chi_\pi \pi_t + \chi_x (y_t - y_t^n)] + \varepsilon_t^{MP} + v_{1,t-1}, & \text{for } s = 0, \\ \rho i_{t-1+s} + (1 - \rho) [\chi_\pi \mathbb{E}_t(\pi_{t+s}) + \chi_x \mathbb{E}_t(y_{t+s} - y_{t+s}^n)] + v_{s+1,t-1} + \varepsilon_{s,t}^{FG}, & \forall s \in \{1, 2, \dots, L-1\}, \\ \rho i_{t-1+s} + (1 - \rho) [\chi_\pi \mathbb{E}_t(\pi_{t+s}) + \chi_x \mathbb{E}_t(y_{t+s} - y_{t+s}^n)] + \varepsilon_{s,t}^{FG}, & \text{for } s = L, \\ \rho i_{t-1+s} + (1 - \rho) [\chi_\pi \mathbb{E}_t(\pi_{t+s}) + \chi_x \mathbb{E}_t(y_{t+s} - y_{t+s}^n)], & \forall s > L. \end{cases} \quad (23)$$

Hence, the expression in (23) shows that—consistent with expectations about inflation and economic activity—expectations on the future path of the interest rate should shift in response to announcements of anticipated (forward guidance) monetary policy shocks helping us tease them apart from unanticipated (surprise) monetary policy shocks. Given this, we adopt the survey-based identification strategy explored by [Doehr and Martínez-García \(2015\)](#) in a VAR setting and employed by [Cole and Milani \(2017\)](#) within a DSGE model which consists in augmenting the vector of observables $Y_t = [y_t, \pi_t, i_t]'$ with survey-based forecasts with which to disentangle anticipated from unanticipated monetary policy shocks.¹⁵

We expand the vector of observables Y_t with expectations as follows:

$$\bar{Y}_t = [y_t, \pi_t, i_t, \mathbb{E}_t(\Delta y_{t+1}), \mathbb{E}_t(\Delta y_{t+2}), \mathbb{E}_t(\pi_{t+1}), \mathbb{E}_t(i_{t+1}), \dots, \mathbb{E}_t(i_{t+L})]', \quad (24)$$

where $\Delta y_{t+j} = \Delta x_{t+j} + \Delta y_{t+j}^n$ denotes the growth rate of actual output at time $t + j$ (for $j = 1, 2$) and, by analogy, we define $\Delta y_{t+j}^n = (y_{t+j}^n - y_{t+j-1}^n)$ to be the corresponding growth rate of output potential at time $t + j$.¹⁶ Given the structure of the economy described by equations (9) – (10), the non-monetary shock processes in (11) – (14), the [Taylor \(1993\)](#) rule

¹⁴Alternatively, we could also use the yield curve to help us identify the news shocks. Assuming the expectations hypothesis of the terms structure of interest rates holds, it follows from equations (16) and (23) that the long-term nominal interest at any given maturity $n \geq L + 1$ (i_t^n) can be expressed as:

$$i_t^n = \rho \left(\frac{1}{n} \sum_{z=0}^{n-1} \mathbb{E}_t i_{t-1+z} \right) + (1 - \rho) \left[\chi_\pi \left(\frac{1}{n} \sum_{z=0}^{n-1} \mathbb{E}_t \pi_{t+z} \right) + \chi_x \left(\frac{1}{n} \sum_{z=0}^{n-1} \mathbb{E}_t x_{t+z} \right) \right] + \frac{1}{n} \left(\varepsilon_t^{MP} + v_{1,t-1} + \sum_{l=1}^L v_{l,t}^{FG} \right).$$

Working directly with the expected path of the policy rate, as we do in this paper, lessens the concern that using longer maturity rates along the yield curve means that we are jointly testing the validity of our model and also that of the expectations hypothesis of the term structure of interest rates at the same time.

¹⁵In [Subsection 2.3](#), we show how to model aggregate expectations that mixes FIRE and VAR-based expectations and subsequently also explain how we relate model expectations to the observed survey-based forecasts.

¹⁶In estimations, we use up to five periods ahead of the interest rate forecasts as part of our observables (i.e., up to $\mathbb{E}_t(i_{t+5})$) given the data available in the SPF dataset. The corresponding observation equations will be described in more detail in [Subsection 3.2.1](#).

in (22), and the unanticipated and anticipated monetary policy shocks given by (17) – (21), hence the vector of expectations-augmented observables \bar{Y}_t in (24) suffices to ensure that we can identify all structural shocks $\varepsilon_t = \left(\gamma_t, \mu_t, \varepsilon_t^{MP}, \{\varepsilon_{l,t-l}^{FG}\}_{l=1}^L \right)'$.

2.3. Central Bank Credibility

Forward guidance opens up the possibility for central banks to manage expectations but is inherently time-inconsistent (Kydland and Prescott (1977)). That is because forward guidance ultimately are promises about future monetary policy that the central bank may find beneficial to renege from unless future policymakers could be bound somehow to credibly honor those commitments when the time comes.

This is partly because, while the vector of observables $Y_t = [y_t, \pi_t, i_t]'$ can be monitored with observable data, neither announcements about the expected future path of the policy rate (news shocks) nor the central bank’s own public forecasts—if used to communicate the forward guidance policy—can be monitored and validated in real-time with the observed current data Y_t or its lags at the time the announcement is made. It is also partly because central banks have incentives to deviate from those commitments.

Simply put, private agents realize that there is neither a full-proof verification mechanism nor a way to enforce those promises to guarantee that the monetary policymakers deliver on the future policy path that has been promised and, therefore, private agents must form expectations accordingly. In other words, private agents have to factor the credibility of the central bank’s forward guidance future policy commitment in forming their own expectations about the future.

We assume that private agents believing the central bank’s commitments form their expectations under the fully-informed, rational expectations (FIRE) paradigm recognizing the aggregate implications of the credibility of those policy commitments. Private agents believing the central bank’s commitments not to be credible form their expectations about the observables using a standard VAR model and commit themselves to forecast the future path of the economy’s macro aggregates in that way (ignoring all announcements until they materialize—if they do—at a later time). That is, private agents forecast the observable vector $Y_t = [y_t, \pi_t, i_t]'$ with the following parsimonious structural VAR(1) process in mind:

$$Y_t = A + BY_{t-1} + u_t, \tag{25}$$

which captures well the historical dynamics of Y_t in our sample. Here, A and B are reduced-

form matrices of conforming dimensions, and u_t is a vector of (non-structural) residuals.¹⁷

Following on the footsteps of the axiomatic approach for heterogenous beliefs of [Branch and McGough \(2009\)](#), aggregate expectations ($\mathbb{E}_t(Y_{t+1})$) are a weighted sum of expectations from private agents who believe the central bank to be credible and those who do not.¹⁸ Specifically, we define aggregate expectations as follows:

$$\mathbb{E}_t(Y_{t+1}) = \tau \mathbb{E}_t^C(Y_{t+1}) + (1 - \tau) \mathbb{E}_t^D(Y_{t+1}), \quad (26)$$

where $\mathbb{E}_t^C(Y_{t+1})$ represents the FIRE forecasts of macro variables of private agents that view the central bank’s commitments as fully credible and $\mathbb{E}_t^D(Y_{t+1})$ denotes the expectations of private agents who believe the monetary authority’s commitment to be not credible. As stated above, the latter form expectations based on equation (25). Equation (26) also follows [Haberis et al. \(2019\)](#) who model aggregate expectations as a weighted average of FIRE and VAR forecasts.

The parameter $0 < \tau < 1$ determines the odds placed on $\mathbb{E}_t^C(Y_{t+1})$ or, alternatively, the share of private agents that forms FIRE expectations. We refer to τ as the credibility parameter of the model.¹⁹ In the limiting case where $\tau = 1$, all private agents in the economy believe the central bank to be perfectly credible and expectations to be homogeneous across

¹⁷In our estimation, the parameters of A and B in (25) would be recovered jointly as part of the full structural model. Therefore, the resulting estimates reflect the information available over the full sample. We leave the issue of learning about A and B , and its stability properties, for future research.

¹⁸We assume households own the firms and we therefore refer to the firm-owning households as private agents. This implies that, in our benchmark economy, the expectations of households will not differ from those of firms that enter into the aggregate demand and price-setting behavior equations in equilibrium. We leave for future research the exploration of richer environments where firms’ expectations may differ from those of households.

¹⁹There are different ways to motivate theoretically the credibility parameter $0 < \tau < 1$. In this paper, we suggest a theoretical interpretation based on the equilibrium of a game-theoretic framework between rational-expectations private agents and the central bank through the lens of an evolutionary-type “game of chicken” ([Osborne and Rubinstein \(1994\)](#)). This credibility game is presented in the [Appendix](#) which provides all the necessary details about its structure and solution. However, for our estimation purposes what is most crucial is that lack of credibility can contribute to the emergence of heterogeneous expectations. We posit that, under imperfect credibility, there is at least a fraction of agents in the economy making forecasts that abstract from monetary policy announcements (as is the case for those agents using VAR-based forecasts in our setup). Credibility in this more broad sense is something to be earned by policymakers. Forward guidance commitments are essentially costless for private agents to take almost irrespective of how they form expectations, if fully credible. If forward guidance commitments are believed and are thought to be effective, then private agents would be making systematic errors using VAR-based forecast instead which puts them at a disadvantage and so they would be more likely to act like FIRE agents do by simply conforming to the central bank’s guidance. Implicitly, therefore, what we are saying is that heterogeneous beliefs arise when the agents recognize that the central bank can renege on its commitments which would lead them to commit systematic errors if the policy announcements were factored at face value in forming their expectations.

all agents (i.e., $\mathbb{E}_t Y_{t+1} = \mathbb{E}_t (Y_{t+1}^C)$). In the opposite polar case where $\tau \rightarrow 0$, the monetary authority is considered not to be credible and homogeneous beliefs imply that $\mathbb{E}_t (Y_{t+1}) \rightarrow \mathbb{E}_t^D (Y_{t+1})$.

Our specific choice of modeling credibility with equation (26) is partly motivated by prior research and comparability reasons. [Bernanke et al. \(2019\)](#) study imperfect credibility with FRB/US, the main simulation model of the Federal Reserve. Similar to our equation (26), aggregate expectations in the previous authors’ paper are assumed to be composed of model-consistent FIRE expectations and forecasts based on a VAR that ignores Federal Reserve announcements (as in our model with imperfectly credible guidance). The description of credibility in [Yellen \(2006\)](#) also seems akin to our definition. [Yellen \(2006\)](#) describes central bank credibility as agents correctly anticipating policy in response to economic shocks. Thus, lack of credibility could be understood as not incorporating Federal Reserve future policy announcements into forecasts, similar to what we do in equation (25). [Blinder \(2018\)](#) also states that agents not incorporating monetary policy communication into their forecasts are effectively acting as if they do not believe the monetary authority.

In addition, we argue that incorporating heterogeneous expectations is crucial to reconcile the model with the survey evidence. That empirical evidence seems to run *contrary* to a model with homogeneous expectations where all agents are fully-informed rational, and their forecasts align with those of the central bank. As a way of illustrating this point, we look at how since 2012 the Federal Reserve has communicated its “Delphic” guidance via dot plots for the fed funds rate as part of the Fed’s Summary of Economic Projections (SEP).²⁰ We compute the median SEP value of the fed funds rate from those dot plots for the current year and the following two years. We match each observation of the median SEP with the time-consistent individual forecast of the 3-month interest rate from the Survey of Professional Forecasters (SPF), for each forecasting horizon. We then calculate the pooled median and the 75th - 25th percentile range of the individual SPF forecasts for each forecasting horizon and illustrate how those ranges relate with the SEP median in [Figure 1](#).

The results shown in this figure display notable discrepancies between the median SEP and median SPF forecasts and the sizeable dispersion of the individual SPF forecasts themselves. We argue that allowing for heterogeneous expectations would not be enough, as relying on the central bank’s communication about the interest rate path is the costless path to follow for everybody irrespective of whether or not agents are fully-informed and rational, unless agents are concerned about the credibility of those announcements (or for

²⁰Dot plots are used by the Fed to convey its outlook on the benchmark fed funds rate at four Federal Open Market Committee (FOMC) meetings per year.

some reason choose to act sub-optimally relying on other likely worse forecasts for the policy rate). Even if forward guidance announcements are deemed perfectly credible, the forecasts of agents who are neither fully rational nor fully informed would tend to coalesce around the policy path announced by monetary authorities as this does not require any costly effort to acquire or process the information. However, as shown in [Figure 1](#), the empirical forecasts for private agents do not appear to coalesce around their SEP median counterparts either.²¹

We must recognize also that, while heterogenous beliefs can result from different causes, our structural model only allows considers the case where heterogenous expectations appear as a result of imperfect credibility about the forward guidance announcements. How do we know this? Because the VAR representation accounted for in equation (25) is just a reduced-form representation of the solution of the structural model absent the forward guidance news shocks (see, e.g., [Martínez-García \(2018\)](#)). In effect, the VAR solution representation in equation (25) is not inconsistent with the structural solution that would occur if the structural model is solved in the case where all agents decided not to believe forward guidance news and only responded to monetary shocks when they materialize.

Forward Guidance Credibility and the Modeling Structure. In general, aggregate expectations of private agents would be a convex combination weighed by a parameter τ that lies within the unit interval. This is the benchmark model we estimate in this paper and inevitably leads to an economy where forward guidance loses some of its power if τ is strictly less than one.

We choose to study forward guidance and central bank credibility with a relatively smaller scale New Keynesian model to avoid the danger of overparameterization. Using a larger scale model (e.g., [Smets and Wouters \(2007\)](#)) would incorporate a richer set of equilibrium relationships, but also would necessitate additional observables and shocks in the estimation to help identify a larger set of deep structural parameters. Moreover, the number of structural parameters to estimate in equation (25) would expand. As discussed in [Stock and Watson \(2001\)](#), the potential issue with too many parameters is unreliable estimates. Thus, while it is indeed important to consider a larger-scale DSGE model that captures more of the equilibrium relationships between the variables, we limit the scope of our paper to examine the efficacy of forward guidance under imperfect credibility through the benchmark

²¹We also should note that we do not have data with which we can explore the decision of the policymaker to announce and then renege or not forward guidance commitments. If we had forecast data from the Fed itself for a long enough period of time, perhaps we would be able to perform an exercise along those lines. In the present case, we cannot do so and that entails that we cannot flesh out that distinction. We believe, however, that the conclusions about monetary policy credibility are still very relevant.

model presented earlier. We leave the exploration of a larger-scale DSGE model for future research.²²

3. Bayesian Estimation Methods

The workhorse New Keynesian model with forward guidance and central bank credibility that we have laid out here includes equations for aggregate demand (the dynamic IS curve), the New Keynesian Phillips curve (NKPC), potential output, the frictionless real interest rate (or natural rate), and the AR(1) processes for the productivity growth shock and for the cost-push shock. Moreover, the model is completed with a [Taylor \(1993\)](#) monetary policy rule with inertia and surprise monetary policy shocks, forward guidance (news) shocks, and a recursive representation of the central bank’s promises regarding changes to future interest rates (announcements). The private agents’ expectations are based on a VAR if the central bank is not viewed as credible and based on FIRE expectations if credible, while heterogenous-beliefs aggregate expectations are weighted by a central bank’s credibility parameter. In other words, the benchmark model that we estimate includes equations (9), (10), (11), (12), (13), (14), (16), (19) – (21), (25), and (26). We implement our estimation strategy and approach using Dynare codes ([Adjemian et al. \(2011\)](#)).

3.1. Data Sources

We utilize Bayesian estimation techniques with U.S. macroeconomic time series variables at a quarterly frequency. Data for output, inflation, and interest rates correspond to U.S. real GDP growth, the growth rate in the GDP deflator, and the fed funds rate. The relevant acronyms are GDPC1, GDPDEF, and FEDFUNDS with the data retrieved from the FRED database of the Federal Reserve Bank of St. Louis. We also employ observations for expectations of future macroeconomic variables. Specifically, we utilize expectations regarding one-quarter and two-quarters ahead output growth, one-quarter ahead inflation, and one-quarter to five-quarters ahead interest rates. These forecast series are retrieved from the Survey of Professional Forecasters (SPF) database of the Federal Reserve Bank of Philadel-

²²With that being said, it should also be stated that we include a number of frictions and rigidities (i.e., habit formation in consumption, price stickiness, price indexation, and interest rate inertia) in our benchmark model beyond the simple three equation New Keynesian model in order to better align the model with the data.

phia (FRB of Philadelphia (2019)).²³ The relevant acronyms are RGDP, PGDP, and TBILL. In addition, our dataset spans the period from 1981 : Q3 through 2017 : Q3 with forecasts going up to 2018 : Q4.²⁴

3.2. Estimation Strategy

3.2.1. Observation Equations

The observation equations mapping the model variables into the data are given by the following system of equations:

$$\begin{bmatrix} g_t^{obs} \\ \pi_t^{obs} \\ i_t^{obs} \\ \mathbb{E}_t^{obs}(g_{t+1}) \\ \mathbb{E}_t^{obs}(g_{t+2}) \\ \mathbb{E}_t^{obs}(\pi_{t+1}) \\ \mathbb{E}_t^{obs}(i_{t+1}) \\ \mathbb{E}_t^{obs}(i_{t+2}) \\ \mathbb{E}_t^{obs}(i_{t+3}) \\ \mathbb{E}_t^{obs}(i_{t+4}) \\ \mathbb{E}_t^{obs}(i_{t+5}) \end{bmatrix} = \begin{bmatrix} \Delta y_t \\ \pi_t \\ i_t \\ \mathbb{E}_t(\Delta y_{t+1}) \\ \mathbb{E}_t(\Delta y_{t+2}) \\ \mathbb{E}_t(\pi_{t+1}) \\ \mathbb{E}_t(i_{t+1}) \\ \mathbb{E}_t(i_{t+2}) \\ \mathbb{E}_t(i_{t+3}) \\ \mathbb{E}_t(i_{t+4}) \\ \mathbb{E}_t(i_{t+5}) \end{bmatrix} + \begin{bmatrix} \bar{\gamma}^g + \gamma_t \\ \bar{\gamma}^\pi \\ \bar{\gamma}^r \\ \bar{\gamma}^{g^1} + \mathbb{E}_t(\gamma_{t+1}) \\ \bar{\gamma}^{g^2} + \mathbb{E}_t(\gamma_{t+2}) \\ \bar{\gamma}^\pi \\ \bar{\gamma}^{r^1} \\ \bar{\gamma}^{r^2} \\ \bar{\gamma}^{r^3} \\ \bar{\gamma}^{r^4} \\ \bar{\gamma}^{r^5} \end{bmatrix} + \begin{bmatrix} \mathbf{0}_{3 \times 8} \\ \mathbf{I}_{8 \times 8} \end{bmatrix} \begin{bmatrix} o_t^{g_{t+1}} \\ o_t^{g_{t+2}} \\ o_t^{\pi_{t+1}} \\ o_t^{i_{t+1}} \\ o_t^{i_{t+2}} \\ o_t^{i_{t+3}} \\ o_t^{i_{t+4}} \\ o_t^{i_{t+5}} \end{bmatrix}, \quad (27)$$

where $g_t \equiv \Delta y_t$ represents the growth rate of output at time t . Observations for expectations include *i.i.d.* measurement error terms, i.e., $o_t^{g_{t+1}}$, $o_t^{g_{t+2}}$, $o_t^{\pi_{t+1}}$, $o_t^{i_{t+1}}$, $o_t^{i_{t+2}}$, $o_t^{i_{t+3}}$, $o_t^{i_{t+4}}$, and $o_t^{i_{t+5}}$. This mapping is similar to that of Cole and Milani (2017) and consistent with the expectations-augmented approach to disentangle between news and surprises about monetary policy proposed by Doehr and Martínez-García (2015).

²³We use the mean value across respondents because it conforms with the notion of aggregate forecasts implied by equation (26). However, our results are largely robust if we instead use the median value.

²⁴Notice that forward guidance outside the explicit forward guidance statements that emanated in the aftermath of the 2007 – 09 global financial crisis can still be present in our full dataset. Campbell et al. (2012) explain that the FOMC has issued implicit and explicit forward guidance long before the 2007 – 09 global financial crisis. Lindsey (2003) also discusses types of central bank communication in the 1980s in the U.S. Wynne (2013) explains how FOMC statements to the public have evolved from vague text in the early 1990s to more specific and clarifying statements post-2009. Contessi and Li (2013) also discuss FOMC statements containing elements of forward guidance in the early 2000s. BIS (2019) provides a detailed description and assessment of forward guidance and other monetary policy tools since the 2007 – 09 global financial crisis for the U.S. and across other countries with related experiences.

It is important to clarify how the SPF expectations align with model implied expectations. From the SPF documentation (FRB of Philadelphia (2019)), the respondents of the SPF usually have to report their forecasts before the middle of the current quarter. For instance, in regards to forecasts for $Q1$, the deadline submission date is the second to third week of February. The nowcast is approximately a 2-month ahead forecast while the one-quarter ahead is a 5-month ahead forecast and so on. For that reason, a number of papers in the literature most closely connected to ours map the nowcast of the forecasted variables of the SPF as the one-quarter ahead forecast in the model (e.g., that of Cole and Milani (2017)). In our baseline analysis, we also treat the SPF nowcast as corresponding to the one-quarter ahead forecasts in our benchmark model to ensure comparability.²⁵ However, in Subsection 5.3, we analyze the baseline results under a different (but still plausible) timing convention using instead one-quarter ahead SPF forecasts as the one-quarter expectations in the model.

3.2.2. Choice of Priors

The choice of prior distributions on the structural parameters largely follows Smets and Wouters (2007) and Cole and Milani (2017).²⁶ The price indexation parameter ι_p is assumed to have a prior distribution of Beta. We select a Normal distribution centered over 1 for the prior distribution of the inverse of the Frisch elasticity of labor supply ω . We also assume persistence in the productivity growth and cost-push shocks as these both have Beta prior distributions with mean of 0.50. To ensure positive values, the prior distributions on the standard deviations of the shocks are chosen to be Inverse Gamma.

The prior distribution of the policy parameters are also standard from prior studies. The priors on the χ_π and χ_x are both Normal centered over 1.5 and 0.125, respectively. We assume there exists a high degree of persistence *a priori* when the central bank adjusts the interest rate as ρ follows a Beta with mean 0.75. The prior assumptions on the previous three parameters follow from Smets and Wouters (2007). In addition, the value of the forward guidance horizon is chosen to be twelve periods, that is, $L = 12$. This assumption is based on the FOMC statement utilizing time-contingent (calendar-based) forward guidance.

²⁵As we utilize the nowcast for $t + 1$ expectations, we have SPF data for the nowcast and up to four-quarters ahead for the estimation (which we exploit to its fullest). Hence, in the benchmark model, equation (27) includes up to five periods ahead interest rate expectations (i.e., $\mathbb{E}_t^{obs}(i_{t+1})$, $\mathbb{E}_t^{obs}(i_{t+2})$, $\mathbb{E}_t^{obs}(i_{t+3})$, $\mathbb{E}_t^{obs}(i_{t+4})$, and $\mathbb{E}_t^{obs}(i_{t+5})$).

²⁶The following parameters are fixed: the household's intertemporal discount factor β is set to 0.99, habit persistence η is fixed at 0.50, and the composite coefficient ξ_p is set to 0.0015. The latter two values roughly follow Cúrdia et al. (2015) and Giannoni and Woodford (2004), respectively. The constants in the observation equations in (27) are fixed to the historical mean of their respective series.

Specifically, in September 2012, the FOMC stated “the Committee also . . . anticipates that exceptionally low levels for the federal funds rate are likely to be warranted at least through mid-2015.” Thus, there are twelve quarters from September 2012 and “mid-2015” if the latter date is taken to be the end of quarter three of 2015.

The central parameter in our model is τ which measures the degree of central bank credibility in the economy. As described above, all agents in the economy believe central bank statements to be perfectly credible whenever $\tau = 1$. If $\tau \rightarrow 0$, the central bank is not perceived to be credible and agents do not factor forward guidance statements into their forecasts. In our benchmark estimation, we choose an informative prior distribution, a Beta prior with mean 0.8 based on ancillary evidence. To support this, we note that private forecasts tend to strongly and positively comove with the path indicated by the Fed even if the comovement is not perfect with the Fed’s own across individual forecasters (as seen in [Figure 1](#)). However, as this parameter τ is central to our analysis, we will conduct some robustness checks in [Subsection 5.2](#). Specifically, we compare the baseline results to the case if one is more agnostic about the true value of τ and adopts a less informative distribution.

3.2.3. Reduced-Form Forecasting Model

The current paper assumes that expectations for the entire economy are composed of a weighted sum of FIRE expectations and VAR-based expectations that simply ignore the forward guidance statements. As stated in equation (25), the latter type of agents form expectations via a VAR(1) process. However, it is important to motivate the lag length of this forecasting model. To accomplish this task, we calculate the Bayes Information Criterion (BIC) for a VAR(1), a VAR(2), and a VAR(3) model on the vector of observables $Y_t^{obs} = [g_t^{obs}, \pi_t^{obs}, i_t^{obs}]$.²⁷ The BIC values for the three models are -31.16 , -20.05 , and 4.56 , respectively. Thus, we utilize the VAR(1) as it has the lowest BIC.

4. Main Results

4.1. Estimates of Central Bank Credibility

We now proceed with our main empirical exercise to investigate the effects that central bank credibility has on the efficacy of forward guidance. When we estimate τ , we refer to this case as the not perfectly credible central bank scenario, and denote the estimate as $\hat{\tau}$.

²⁷For this, we use data spanning 1985 : Q1 through 2007 : Q3. This period corresponds to the Great Moderation era in the U.S.

When we do not estimate τ and assume private agents perceive the monetary authority to be perfectly credible, we simply set the credibility parameter to be $\tau = 1$ in the estimation. The results are shown via three channels: posterior point estimates, variance decomposition, and impulse response functions under both perfectly credible and imperfectly credible central bank scenarios.

Table 1 and Table 2 display the posterior mean and 90% highest posterior density interval estimates. Table 3 shows the conditional variance decomposition upon impact of the forward guidance and all other structural shocks with parameter values at their posterior mean. The last line calculates the sum of all the variation in the macroeconomic variable due to the forward guidance shocks. Figure 2 and Figure 3 display the impulse response functions to forward guidance shocks at different horizons while Figure 4 displays the impulse response functions for the productivity growth, cost-push, and unanticipated monetary policy shocks. Each panel shows the mean response of the model-implied output and the other macro observables (inflation and interest rate). The solid line represents the scenario where $\tau = 1$, while the dashed line denotes $\hat{\tau}$.

We first examine the case in which the monetary authority is perceived to be perfectly credible. In Table 1 and Table 2 the first three columns under “Posterior Distribution” show that the estimates of the main structural parameters largely align with prior literature. The estimated value of the inverse of the Frisch elasticity of labor supply $\omega = 0.97$ follows closely that of Cúrdia et al. (2015). The interest rate smoothing parameter is estimated to be high at 0.88 which closely aligns with the value found in Milani (2007) using a model with FIRE expectations. The estimates for the degree of productivity growth inertia (ρ_γ) and inflation indexation (ι_p) roughly follow the results found in Cúrdia et al. (2015) under their “W” rule.²⁸

The solid lines in Figure 2 and Figure 3 show the mean impulse response whenever $\tau = 1$ to a one standard deviation increase in a shock. Specifically, given that agents are forward looking, news that the interest rate will increase 1, 4, 8, or 12 periods ahead affects agents’ intertemporal decisions by (noticeably) lowering output and inflation on impact. When the shock is realized on the economy, output (roughly) reaches its trough. Since those who perceive the monetary authority to be perfectly credible form their expectations under FIRE, these agents completely understand the shock has already materialized, and thus, output, inflation, and interest rates proceed to return back to steady state.²⁹

²⁸The posterior mean estimate for σ_γ is relatively lower than in Cúrdia et al. (2015). However, this low value could be due to the inclusion of forward guidance shocks and heterogenous expectations in the present paper that do not feature in their model.

²⁹The relative smoothness of the output impulse responses could be due to a mixture of habits in con-

What are the predicted effects if the central bank is not assumed to be perfectly credible? To answer this question, we first analyze the posterior estimates in the last three columns in [Table 1](#) and [Table 2](#). Overall, the values of the main structural parameters do not drastically differ from the perfectly credible case, but do display a few slight differences. For instance, in the last three columns under “Not Perfectly Credible C.B.,” the estimated value of the autoregressive parameter on the cost-push shock is relatively lower than in the $\tau = 1$ scenario. However, this lower persistence could instead be picked up by the higher estimates for the inflation indexation parameter relative to the perfectly credible central bank case.³⁰

More importantly, when allowing private agents the option of not fully believing forward guidance statements about the path of interest rates, the estimate of the credibility parameter τ is 0.77. This value indicates a certain level of trust in the U.S. central bank (i.e., the Federal Reserve) implying some effectiveness of forward guidance on the economy.³¹ However, the fact that this estimated value is not close to $\tau = 1$ suggests that private agents do not believe the monetary authority to be perfectly credible (or at least act in forming their expectations as if monetary policy announcements were not fully credible).

The ramifications of this result are a dampening of the power of forward guidance on the economy. [Figure 2](#) and [Figure 3](#) display this outcome. The impulse responses under $\hat{\tau}$ (dashed line) follow similar paths as under $\tau = 1$ (solid line). However, the dashed line is not as reactive to central bank forward guidance as the solid line. Specifically, the initial impact of output and inflation to forward guidance news is larger under the perfectly credible case than under the imperfectly credible scenario. When the forward guidance shock is realized on the economy l periods later, the responses of output and inflation are also overall larger under $\tau = 1$ than $\hat{\tau}$. The reason for the discrepancies is that private agents believe central bank statements about future interest rates under the $\tau = 1$ scenario, and thus, fully internalize the effects of forward guidance. In contrast, agents who do not fully believe forward guidance commitments do not incorporate the full effects of forward guidance, and thus, macroeconomic variables are not as responsive.

Variance decomposition results also display the diminished effects of forward guidance on the economy under an imperfectly credible monetary authority. In [Table 3](#) we compute

sumption and the fact that when private agents believe the forward guidance statements to be fully credible anticipate their decisions accordingly before the shock materializes l periods later.

³⁰The parameter ρ_γ is also estimated to be lower than under the $\tau = 1$ scenario. This result comes in hand with the fact that the standard error of the productivity shock has a higher value under $\hat{\tau}$ than under $\tau = 1$.

³¹This result does agree with [Swanson \(2018\)](#) who finds that forward guidance indeed has a degree of effectiveness when the economy is constrained by ZLB.

the conditional variance decomposition upon impact of the shocks with parameter values at their posterior mean. The combined contribution of the forward guidance shocks to output and inflation is less under $\hat{\tau}$ than $\tau = 1$. Under a central bank that is perceived as imperfectly credible, the total contribution of $\varepsilon_{1,t}^{FG}$, $\varepsilon_{2,t}^{FG}, \dots, \varepsilon_{12,t}^{FG}$ to output and inflation is 7.53% and 0.00%, respectively.³² Under a monetary authority perceived as perfectly credible, the combined contribution is 23.14% and 1.36%. Thus, if a central bank is perceived as more credible, there exist greater immediate effects on the real economy from forward guidance but with little effect on inflation. To put it another way, if the central bank is less credible, the immediate effects on output are not as great relative to the perfectly credible scenario.

The results show that modeling forward guidance credibility contributes to dampen the large effects that led [Del Negro et al. \(2012\)](#) to question the magnitudes of these anticipation effects in the New Keynesian (which these authors termed the “forward guidance puzzle”). In their paper, [Del Negro et al. \(2012\)](#) explain that a standard New Keynesian model similar to the one presented in [Section 2](#) produces surprisingly large responses of the macroeconomic variables to forward guidance shocks. In contrast, our paper allows for private agents to not perceive the monetary authority as perfectly credible. As discussed in the previous paragraphs, the results show that the reaction of macroeconomic variables to forward guidance shocks is dampened and therefore is not as sizeable under $\hat{\tau}$ relative to $\tau = 1$.

The prior literature has offered different views on the “forward guidance puzzle”. For instance, [Del Negro et al. \(2012\)](#) show unusually large responses of the macroeconomic variables to forward guidance via a constant interest rate scenario. [Bundick and Smith \(2020\)](#) and [Kiley \(2016\)](#) utilize elasticities of output relative to a change in future interest rates when comparing model- and data-implied forward guidance effects.³³ [McKay et al. \(2016\)](#) present the puzzle via a one-period anticipated interest rate shock occurring at time T in the future, which is similar to our current analysis. However, they analyze the effects of forward guidance under complete and incomplete asset markets, whereas we focus on forward guidance credibility (or lack thereof) of the central bank.

In all of these cases, the point of reference is somewhat different and the quantification and interpretation are also a bit different as a result. Hence, it is hard to make an apples-to-apples comparison across the different contributions to the literature on the forward guidance puzzle to neatly show how our results compare. Moreover, in all previous cases the results

³²Without rounding the numbers, it should be noted that the contribution of each of the forward guidance shocks to inflation is a small, positive number. This low value agrees well with the response of inflation upon impact to forward guidance shocks found in the impulse response graphs (i.e., [Figure 2](#) and [Figure 3](#)).

³³[Bundick and Smith \(2020\)](#), in particular, do compare quantitative effects on output from forward guidance using a VAR and standard DSGE models.

are model-dependent and, to our knowledge, none of the previous estimates have explored the potential role of credibility and heterogeneous expectations. Nevertheless, we compute elasticities of output and inflation to a change in expected interest rates four-periods ahead which is a similar conceptual exercise to what [Bundick and Smith \(2020\)](#) do. Specifically, we divide the trough response of output (inflation) to a four-period ahead forward guidance shock as seen in [Figure 2](#) by the initial response of (observed) expected interest rates four-periods ahead. We compute these statistics across both the $\tau = 1$ and $\hat{\tau}$ cases.

[Table 5](#) shows that the elasticities of output are -5.28 and -0.65 under the $\tau = 1$ and $\hat{\tau}$ scenarios, respectively. In other words, under perfect credibility, a one percentage point increase in expected four-quarter ahead interest rates is associated with a 5.28 percentage point drop in output at its trough point. Under imperfect credibility, the maximum decrease in output is 0.65, confirming our benchmark results that assuming a perfectly credible central bank can overstate the predicted effects of forward guidance on the economy. The elasticities of inflation are also -0.10 and -0.03 under the $\tau = 1$ and $\hat{\tau}$ scenarios, respectively. We also should note that the elasticity numbers for the $\hat{\tau}$ scenario are less than the values found in [Bundick and Smith \(2020\)](#). We attribute the difference, at least in part, to the fact that their analysis implicitly assumes fully credible forward guidance commitments. In our paper, we have argued and shown that the credibility assumption greatly affects the efficacy of forward guidance on the economy as seen in [Table 5](#) as well as in [Figure 2](#) and [Figure 3](#).

Overall, the results of our main exercise suggest a number of takeaways. Our estimate of the Federal Reserve’s credibility is high at $\hat{\tau} = 0.77$. However, this estimated value is below the fully credible case which leads to an attenuation of the power of forward guidance. If the central bank is perceived as less credible, there exist less immediate and overall effects on the economy from forward guidance. Hence, the integration of imperfect central bank credibility into a standard macroeconomic model can be another feature of the economy that contributes to mute the effects of forward guidance. Thus, accounting for imperfect credibility is important to model the formation of expectations in the economy and the transmission mechanism of forward guidance announcements.

4.2. Evidence That τ Reflects Central Bank Credibility

The present paper models aggregate expectations as a weighted average of those who believe central bank forward guidance statements as fully credible and those that do not. The former group forecasts macroeconomic variables under the assumption of FIRE, while the latter uses a data-driven VAR(1) model. In equation (26), the parameter τ measures the

degree of central bank credibility in terms of forward guidance. This parameter was taken to be constant and exogenous for simplicity, similar to what the prior literature does (e.g., [Haberis et al. \(2014\)](#)). However, a perennial question regards to what extent τ reflects central bank credibility? To try to explore this question further, we perform three exercises that give us additional confidence that τ is capturing a measure of monetary authority credibility. Specifically, we examine the influence of frictions on the estimate of τ , the influence of the reduced-form forecasting model on τ , and the comovements between forecast errors and forecast disagreements of the SPF dataset relative to those implied by our benchmark model with imperfect credibility.

4.2.1. Alternative Macro Persistence Features

The VAR(1) framework that private agents who do not believe the monetary authority to be credible utilize to construct forecasts involves inherent persistence in the macroeconomic variables. Because our benchmark model incorporates a number of standard macro persistence features (such as habit formation and price indexation) to get at the persistence of the macro variables, it is of interest to investigate if the estimated credibility parameter is sensitive to those features. Intuitively, the hypothesis here is that perhaps the inclusion of macro inertia features may affect the fit of the model at the expense of biasing our estimates of τ . Thus, we analyze the results when habits in consumption (η) and price indexation (ι_p) are turned off and compare it to the baseline outcomes.

First, when habits in consumption are shut off (i.e., $\eta = 0$), the results do not noticeably change. Under the “ $\eta = 0$ ” column, [Table 4](#) displays that the estimate for τ is 0.76, which is virtually identical to our benchmark estimate of 0.77. The posterior mean estimates of the other parameters are largely the same as under the benchmark $\hat{\tau}$ scenario in [Table 1](#) and [Table 2](#). Second, when the degree of price indexation is turned off (i.e., $\iota_p = 0$), the posterior estimates of the parameters are largely unchanged. In particular, the “ $\iota_p = 0$ ” column in [Table 4](#) displays that the estimate of τ at 0.78 is about the same as the benchmark case with price indexation.

Thus, the results shown in [Table 4](#) provide further evidence that our estimate of τ is quite robust to alternative macro persistence features. In other words, τ does not seem to be reflecting a bias from lagged consumption or prices. This does not say that τ is necessarily a good measure of central bank credibility on forward guidance, but it suggests that τ is not making up for the persistence in the data from unmodeled features in our benchmark.

4.2.2. Alternative Reduced-Form Forecasting Model

We also examine the estimation of the central bank credibility parameter τ under alternative specifications of the forecasting models used by the private sector. The benchmark case in [Section 4](#) assumed private sector agents who do not believe the monetary authority to be credible would form expectations from a VAR(1) based on [\(25\)](#). In turn, private agents who believe the central bank followed FIRE expectations. However, a natural question arises regarding whether the estimated value of τ is sensitive to the information set in the forecasting model of private sector agents?

Here, we examine the case when private agents that do not believe the central bank know more about the true structure of the economy. That is, we explore the case when not credible expectations ($\mathbb{E}_t(Y_{t+1}^D)$) become better informed than under [equation \(25\)](#). Private agents are assumed to know the AR(1) productivity and cost-push shock realizations, that is, $w_t = [\gamma_t, \mu_t]'$, when formulating their expectations of future macroeconomic variables. Thus, [equation \(25\)](#) is replaced with:

$$Y_t = A + BY_{t-1} + Cw_t + e_t, \tag{28}$$

where A , B , and C are coefficient matrices of appropriate dimensions, and e_t is a vector of white noise (non-structural) residual terms.

[Table 6](#) and [Table 7](#) produce two main takeaways. First, additional knowledge (or information) about the true structure of the economy seems to have minimal effect on the posterior estimates of the parameters. In [Table 6](#), the estimate of our central bank credibility parameter is 0.78. This value is approximately the same as our baseline estimate of 0.77.³⁴ Thus, even if private agents utilize a forecasting model with more information, the results do not substantially change. In particular, there still are noticeable effects of forward guidance on the economy as private agents are estimated to believe the Fed to be highly credible, although below the fully credible case of $\tau = 1$.

The second takeaway is that, since the estimate of τ does not significantly change when private agents are more informed, τ does not seem to be capturing private agents' lack of knowledge about the true structure of the economy. In other words, it does not seem biased due to not knowing productivity growth and cost-push shocks. Thus, because the value of τ does not seem to depend on these other non-forward guidance elements, this latter result suggests once more that what ultimately underpins τ must be something else like central

³⁴Altogether [Table 6](#) and [Table 7](#) display that the estimates of the other parameters in the model do not appreciably change.

bank credibility on forward guidance.

4.2.3. Predictability of Forecasting Errors

Our benchmark model assumed that expectations in the economy are a weighted sum of private agents who believe the central bank to be perfectly credible and private agents who believe the monetary authority not to be credible. The former group forecasts macroeconomic variables under the assumption of FIRE expectations, while the latter uses a data-driven VAR(1) model. However, a question naturally arises as to whether heterogeneous expectations (with a non-FIRE component) aggregated by τ or the perfectly credible, homogeneous and FIRE expectations case is the more plausible way to describe the observed SPF expectations?

Standard macroeconomic models often consider *only* the $\tau = 1$ case, that is, FIRE expectations. In this scenario, if we take the model to be the true data-generating process, forecast errors will be random and on average equal to zero (see, e.g., [Sims \(2002\)](#) and [Cole and Milani \(2017\)](#)). Moreover, in this case expectations are homogeneous, there are no model-implied forecasting disagreements and thus, forecasting errors would not be dependent or correlated with forecasting disagreements among private agents. However, do the forecast errors from the data agree with those implications of the $\tau = 1$ scenario? Or does the imperfect credibility scenario with $\hat{\tau}$ capturing the estimated central bank credibility fit the SPF data better? To explore these questions further, we compare the forecast errors from our model with imperfect central bank credibility to what is found in the observed SPF forecasting data.³⁵

We proceed in the following manner. We define forecasting errors of the interest rate at the one-quarter ahead horizon as $FE_t^1 = \mathbb{E}_{t-1}(i_t) - i_t$ where the expectations $\mathbb{E}_{t-1}(i_t)$ are being matched to the mean SPF forecast. The remaining forecast errors are defined as $FE_t^2 = \mathbb{E}_{t-2}(i_t) - i_t$, $FE_t^3 = \mathbb{E}_{t-3}(i_t) - i_t$, $FE_t^4 = \mathbb{E}_{t-4}(i_t) - i_t$, and $FE_t^5 = \mathbb{E}_{t-5}(i_t) - i_t$ at the two, three, four, and five-quarters ahead horizons, respectively. Forecasting disagreement (DEV_t^1) at the one-quarter ahead horizon is specified as the difference between the 75th and 25th percentile (i.e., the interquartile range of the SPF data). The remaining forecasting disagreements are given by DEV_t^2 , DEV_t^3 , DEV_t^4 , and DEV_t^5 at the two, three, four, and five-quarters ahead horizons, respectively.

³⁵Indeed, non-random forecast errors have been found in other settings. [Andrade and Le Bihan \(2013\)](#) examine the ECB Survey of Professional Forecasters and [Czudaj and Beckmann \(2018\)](#) study expectations for the G7 countries. Both papers find non-random forecasts errors in the data. [Coibion et al. \(2012\)](#) and [Coibion et al. \(2015\)](#) also test FIRE and show that information rigidities exist in the forecasts of agents.

We collect data from the U.S. economy. Forecasting errors are computed with respect to the mean forecast with SPF data. The relevant acronym is TBILL. Forecasting disagreements are measured with the interquartile range of the cross-sectional distribution of individual forecasts in order to make the empirical results less sensitive to outliers.³⁶ The data span 1981 : Q3 – 2018 : Q4 for the baseline case implying 150 observations. We run separate regressions of FE_t^h on DEV_t^h at the one, two, three, four, and five-quarters ahead horizons ($h = 1, 2, 3, 4, 5$):

$$FE_t^1 = \delta_0^1 + \delta_1^1 DEV_t^1 + e_t^1, \quad (29)$$

$$FE_t^2 = \delta_0^2 + \delta_1^2 DEV_t^2 + e_t^2, \quad (30)$$

$$FE_t^3 = \delta_0^3 + \delta_1^3 DEV_t^3 + e_t^3, \quad (31)$$

$$FE_t^4 = \delta_0^4 + \delta_1^4 DEV_t^4 + e_t^4, \quad (32)$$

$$FE_t^5 = \delta_0^5 + \delta_1^5 DEV_t^5 + e_t^5. \quad (33)$$

The usual regression error terms are described by e_t^1 , e_t^2 , e_t^3 , e_t^4 , and e_t^5 at the one, two, three, four, and five-quarters ahead horizons, respectively.

We perform the same exercise using the simulated counterparts from our model with imperfect central bank credibility and heterogeneous expectations. Specifically, we simulate the model at the posterior mean for a time period of 2,000 observations discarding the first 100 simulated observations. We then perform the same regressions given by equations (29) – (33) on a rolling window of 150 observations.³⁷ We compute our results on 10,000 different draws of the simulated data.

The full range of rolling window estimates are represented in Figure 5, which shows a box-and-whisker plot that displays their min, max, median, and interquartile range. The point estimates obtained from the SPF data are also shown in Figure 5. The orange circles denote estimates of δ_1^1 , δ_1^2 , δ_1^3 , δ_1^4 , and δ_1^5 over the full sample (i.e., 1981 : Q3 – 2018 : Q4). The red diamonds represent estimates from the non-ZLB period of our dataset, that is, from the 1981 : Q3 – 2008 : Q4 subsample.

We first examine what the data would postulate regarding the relationship between forecasting errors and forecasting disagreements. By using SPF data, estimates of δ_1^1 , δ_1^2 , δ_1^3 , δ_1^4 , and δ_1^5 show that forecasting errors are positively correlated with forecasting disagreement.

³⁶We have considered the same exercise where DEV is specified as the difference between the 90th and 10th percentile and similar results occurred.

³⁷The forecasting disagreements like DEV_t^1 are computed as the difference between the highest and lowest forecasts implied by $\mathbb{E}_{t-1}^C(i_t)$ and $\mathbb{E}_{t-1}^D(i_t)$.

The orange circles and red diamonds in [Figure 5](#) are positive and notably display an upward trajectory as the forecast horizon increases. This challenges the assumption that forecasting errors ought to be unpredictable under the perfect credibility case with FIRE expectations whenever $\tau = 1$.

Another implication of the SPF results in [Figure 5](#) is that the mean SPF forecast tends to overestimate the expected path of the U.S. short-term interest rate more whenever disagreement among forecasters is more substantial, and this tends to be more apparent at longer horizons. What occurs when private agents perceive the central bank as not perfectly credible in the model? The simple answer is that the model under $\hat{\tau}$ seems to match the SPF data fairly well on that account too.

In [Figure 5](#), the estimates δ_1^1 , δ_1^2 , δ_1^3 , δ_1^4 , and δ_1^5 using SPF data lie towards the median of their respective box-and-whisker plots under $\hat{\tau}$. The median of the box-and-whisker plots are also in positive territory, which matches their counterparts in the data. In addition, under *both* SPF and simulated data, estimates of δ_1^1 , δ_1^2 , δ_1^3 , δ_1^4 , and δ_1^5 display an upward trend the longer the forecasting horizon. This finding suggests that a model of imperfect credibility and heterogeneous expectations is well-suited to capture forecasting disagreements and the predictability of forecasting errors based on disagreement that we observe in the SPF data.

In short, as noted before, our model of central bank credibility and heterogeneous expectations offers a way to account for the imperfect comovement between the Fed’s forward guidance and the individual projections of private forecasters in the SPF. We hinted at that in [Figure 1](#) for the Fed’s most recent phase of “Delphic” forward guidance. Our imperfectly credible central bank model extends that idea in a flexibly manner to explore the full sample since the onset of the Great Moderation in the 1980s and tease out a common measure of credibility across different strategies (or phases) in the Fed’s use of forward guidance. What we find in [Figure 5](#) is that this theoretical framework matches well key facts of the SPF data. In the SPF, there exists indeed notable disagreements among forecasters which the fully credible central bank model (i.e., the $\tau = 1$ scenario) cannot capture. Furthermore, the fully credible central bank model cannot account for the robust evidence found in the SPF that forecasting errors are predictable on the basis of forecasting disagreements either.

This is not to say that monetary policy credibility explains all forecasting disagreements, but it shows that imperfect credibility is a plausible reason for forecasting heterogeneity that can bring the workhorse New Keynesian model closer to the evidence that we observe in the SPF data.

5. Robustness

A main result of our paper is that the higher the value of the central bank credibility parameter, τ , the greater the effects of forward guidance on the economy. In particular, τ is estimated to be 0.77 for the U.S. economy. This high value implies a higher degree of Federal Reserve credibility as perceived by private agents in the economy, and thus, it implies that the Fed retains a degree of effectiveness from forward guidance. However, the estimated value of τ is below the fully credible case (i.e., below $\tau = 1$).

In the previous section, we showed already that the finding is robust in the presence of macroeconomic persistence features and to an alternative forecasting model used by private sector agents. In the following subsections, we analyze in further detail the robustness of the result. Specifically, we examine the sensitivity of the benchmark outcomes to the time period used in the estimation, the prior beliefs about τ , and the timing assumption matching SPF forecasts to our model's expectations.

5.1. Subsamples

5.1.1. Non-ZLB

Monetary policy was instrumented with the fed funds rate until hitting the ZLB in the aftermath of the 2007 – 09 global financial crisis. It is important to compare the effect of central bank credibility on forward guidance during the non-ZLB and ZLB periods to assess whether our findings are sensitive across subsamples. Thus, in this subsection, we reestimate the model over the subsample 1981 : Q3 – 2008 : Q4 and compare the results to our benchmark outcomes.

The “Non-ZLB” column in [Table 8](#) and [Table 9](#) displays the results. Even during an era where the interest rate does not bind at zero, our baseline result still holds. Specifically, the value of τ is estimated to be 0.78, which is about the same as our benchmark estimate of 0.77. The values of the other parameters do not considerably change either. Therefore, noticeable effects of forward guidance on the economy exist during the non-ZLB period as well as a high degree of Federal Reserve credibility is estimated to exist. However, the estimate of τ still remains below the fully credible central bank scenario.

5.1.2. Great Moderation

Our full sample includes periods of relatively high volatility in the macroeconomic variables (i.e., pre-1985) and to some extent from the 2007 – 09 global financial crisis onward.

Hence, it is also important to examine whether the effect of central bank credibility on forward guidance is the same or not during a more stable time period. Thus, this subsection compares the benchmark estimation to the case in which we reestimate the model over the subsample 1985 : Q1 – 2007 : Q3. This period has been called the “Great Moderation” in which the volatility in macroeconomic variables was relatively low (see, e.g., [Clark \(2009\)](#) and [Martínez-García \(2018\)](#)).

The estimates of the structural and measurement error parameters of this exercise are displayed in the “Great Moderation” column of [Table 8](#) and [Table 9](#). The results show that the benchmark takeaway from [Section 4](#) does not change. The estimate of our central bank credibility parameter is 0.78, which is very similar to our baseline value. Thus, there exists a high degree of central bank credibility in the U.S. during its most stable economic period within the full sample, which provides further evidence that the effect of forward guidance appears largely unchanged over time in the U.S. And, once again, confirms that $\hat{\tau}$ is below the fully credible central bank case.

5.2. Alternative Priors on the Credibility Parameter

Our baseline prior assumption for τ assumed a high degree of central bank credibility. This value seems reasonable and fits well with the Federal Reserve’s strong reputation and the related results in [Park \(2018\)](#) who reports high values for Federal Reserve credibility as well. We have also alluded previously to the evidence in [Figure 1](#). This indicates that while private forecasts do not seem to perfectly coalesce around the Fed’s own projections as we would expect them under the assumption of perfect credibility (and rational and fully-informed central bank forecasters), there is nonetheless evidence of robust comovement that is suggestive that the Fed indeed has the ability to influence the expectations of private forecasters to significant degree. Our prior for τ recognizes that.

However, it is also important to examine our results under a different light, that is, if we were to adopt a more agnostic view about the prior value of τ . In [Table 8](#) and [Table 9](#), we examine the results when the prior distribution for τ changes to an uninformative Uniform distribution on the unit interval. The results show that the estimate for τ in this case is 0.60, which is somewhat smaller than our benchmark of 0.77.³⁸ Therefore, if one is agnostic about the true value of τ and adopts a $U(0, 1)$ prior distribution, similar to the benchmark results in [Subsection 4.1](#), the estimated value of τ is still below the fully credible case (i.e., $\tau = 1$). Moreover, there continues to exist effects of forward guidance on the U.S. economy

³⁸The estimates of the other parameters do not substantially change.

as the public still believes the U.S. central bank to be credible, albeit both the credibility and the magnitude of those effects would be weakened.³⁹

Furthermore, the posterior distributions seem to be similar in shape regardless of the diffuseness of the prior density even when adopt a less informative (more disperse) Beta prior instead than Uniform distribution. The right panel of [Figure 6](#) displays the posterior (solid line) and prior (dashed line) distributions with a $B(0.80, 0.1)$ density assumed *a priori*. The left panel displays the baseline that we use in our estimation, that is, $B(0.80, 0.01)$ for τ . While the mean estimates differ somewhat, the posterior distributions between the more informative and more diffuse prior cases do not appear to overwhelm the posterior distribution on τ . A plot similar to the one for the diffuse prior Beta arises also under the uninformative Uniform prior.

While there is a concern that the parameter τ might be weakly identified, we believe there are valid reasons to defend our benchmark prior—reasons to which we have appealed again at the beginning of this subsection—suggesting the prior should put more mass on higher values of τ . In any event, we interpret the results discussed here as suggesting that the power of forward guidance is overstated under perfect credibility and, if anything, that our baseline estimate of the effects of forward guidance should be viewed as rather *conservative* given that we favor a prior that places more mass on higher values of the credibility parameter.

Our *conservative* baseline estimate of τ already suggests that the power of forward guidance can be significantly dampened under imperfect credibility as seen in [Table 5](#). From our perspective, then, the main takeaway from this is not so much whether the baseline estimate of τ is overstated or not. The main takeaway is that even though we favor the more *conservative* estimate with higher credibility which is what we report as our benchmark, we still find that the higher degree of credibility that we recover from the data (0.77) is still not high enough to produce an impact on economic activity within range of what we would estimate under full credibility.

5.3. Alternative Mapping of SPF Forecasts

[Section 3](#) described the data and observables that we included for the estimation of our model. In our benchmark analysis, we utilized the SPF nowcast for our model’s one-

³⁹A noticeable feature displayed in [Table 8](#) and [Table 9](#) is that the marginal likelihood is also higher under a uniform prior distribution on τ than under the beta prior distribution assumed in our benchmark (in [Table 1](#) and [Table 2](#)). However, the estimate of the main parameter of interest, τ , is only somewhat smaller than the benchmark indicating a still significant degree of central bank credibility is consistent with the data even when utilizing an uninformative prior.

quarter ahead expectations and so on. As explained in [Subsection 3.2.1](#), we believe this assumption made sense given the actual submission dates and timing of SPF forecasts. However, we recognize that questions can emerge regarding this mapping. Specifically, what if SPF one-quarter ahead forecasts were used to correspond with our model's one-quarter ahead expectations instead of the nowcast?

This section performs a robustness check to analyze the results when the above possibility is taken into account. The model's observation equations are modified as follows:

$$\begin{bmatrix} g_t^{obs} \\ \pi_t^{obs} \\ i_t^{obs} \\ \mathbb{E}_t^{obs}(g_{t+1}) \\ \mathbb{E}_t^{obs}(g_{t+2}) \\ \mathbb{E}_t^{obs}(\pi_{t+1}) \\ \mathbb{E}_t^{obs}(i_{t+1}) \\ \mathbb{E}_t^{obs}(i_{t+2}) \\ \mathbb{E}_t^{obs}(i_{t+3}) \\ \mathbb{E}_t^{obs}(i_{t+4}) \end{bmatrix} = \begin{bmatrix} \Delta y_t \\ \pi_t \\ i_t \\ \mathbb{E}_t(\Delta y_{t+1}) \\ \mathbb{E}_t(\Delta y_{t+2}) \\ \mathbb{E}_t(\pi_{t+1}) \\ \mathbb{E}_t(i_{t+1}) \\ \mathbb{E}_t(i_{t+2}) \\ \mathbb{E}_t(i_{t+3}) \\ \mathbb{E}_t(i_{t+4}) \end{bmatrix} + \begin{bmatrix} \bar{\gamma}^g + \gamma_t \\ \bar{\gamma}^\pi \\ \bar{\gamma}^r \\ \bar{\gamma}^{g^1} + \mathbb{E}_t(\gamma_{t+1}) \\ \bar{\gamma}^{g^2} + \mathbb{E}_t(\gamma_{t+2}) \\ \bar{\gamma}^\pi \\ \bar{\gamma}^{r^1} \\ \bar{\gamma}^{r^2} \\ \bar{\gamma}^{r^3} \\ \bar{\gamma}^{r^4} \end{bmatrix} + \begin{bmatrix} \mathbf{0}_{3 \times 7} \\ \mathbf{I}_{7 \times 7} \end{bmatrix} \begin{bmatrix} O_t^{g_{t+1}} \\ O_t^{g_{t+2}} \\ O_t^{\pi_{t+1}} \\ O_t^{i_{t+1}} \\ O_t^{i_{t+2}} \\ O_t^{i_{t+3}} \\ O_t^{i_{t+4}} \end{bmatrix}. \quad (34)$$

Two differences are apparent between the observation equations in this section (i.e., equation (34)) and the baseline observation equations (i.e., equation (27)). First, the $t + 1$ timing in our model now corresponds to one-period ahead expectations in the SPF dataset. In addition, $\mathbb{E}_t^{obs}(i_{t+5})$ is not in equation (34). Since this exercise utilizes one-quarter ahead SPF expectations (and not the nowcast) for $t + 1$ expectations in our model, we only have data up to four-quarters ahead from the SPF under this alternative mapping of survey-based forecasts and model-based expectations. [Table 8](#) and [Table 9](#) display the estimated values of the structural and measurement error parameters for this exercise.

The main takeaway is that the benchmark results are robust to the timing assumption matching SPF forecasts to our model's expectations. The estimated value of our parameter of interest, τ , is 0.78, which does not notably change relative to the benchmark value reported in [Section 4](#). In addition, the estimates of the other parameters do not considerably change either. However, the value of the marginal likelihood is lower at 631.36 compared to 901.18 from the baseline case. Since the marginal likelihood depends on the data, the discrepancy could be due to this implementation using one less observable than that of [Section 4](#) as described in previous paragraph.

6. Conclusion

The aftermath of the 2007 – 09 global financial crisis caused central banks around the world to more explicitly utilize monetary policy forward guidance as a policy tool. However, as we show in this paper, its effectiveness rests on the credibility of the central bank. We jointly model forward guidance (news) shocks, heterogeneous expectations, and central bank credibility, exploiting interest rate expectations and other macro forecasts from the SPF dataset and Bayesian techniques to estimate the credibility of the Federal Reserve’s forward guidance over the 1981:Q3-2018:Q4 period.

The results show a number of important takeaways. First, the estimate of central bank credibility in terms of forward guidance announcements is high for the Federal Reserve indicating a degree of effectiveness of forward guidance on the U.S. economy (particularly for output and much less so for inflation). However, the estimated value is still below the fully credible case. Consequently, when the central bank is perceived to be less than perfectly credible, forward guidance on the economy does less on impact and less overall. Output and inflation do not respond as favorably to forward guidance relative to the fully credible case. Hence, we show that imperfect credibility is an important modeling feature that contributes—at least to some extent—to weaken the strength of the anticipation effects of forward guidance in the workhorse New Keynesian model.

Second, we provide evidence that our model’s expectations framework reflects central bank credibility and aligns well with the SPF data. For instance, our model of imperfect central bank credibility is consistent with the evidence that forecasting errors for the policy path are predictable on the basis of forecasting disagreements among individual forecasters in the SPF. Furthermore, the results on the efficacy of forward guidance on the U.S. economy do not noticeably change when examining the following robustness scenarios: different sample periods, different assumptions on macro persistence, different forecasting models for private sector agents, different priors on the credibility parameter τ , and different timing assumptions regarding SPF forecasts.

Overall, we conclude that accounting for imperfect credibility is important to model the formation of expectations in the economy and the transmission mechanism of forward guidance announcements.

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7. Appendix. An Evolutionary Game of Central Bank Credibility

The private sector chooses between two different pure-strategies that affect how they form their expectations about the future—either they believe the central bank will honor its forward guidance commitments (C) or they disregard the promises that come from announcements about the future path of monetary policy and make forecasts solely on the basis of observable data (D). Similarly, the central bank concerns itself with two pure strategies—either to honor its commitments and deliver on the announced policy (C) or to renege from the existing commitments (D).

Conventionally, the literature on forward guidance has assumed the strategy pair (C, C) holds accepting that such an outcome could be sustained in equilibrium. Indeed, there are conditions on the payoffs of each player that would indeed support such an outcome as an evolutionarily stable strategy (ESS). However, without a payoff-based disciplining mechanism to sustain the strategy pair (C, C) in equilibrium, we must consider the broad range of plausible strategic implications of the non-cooperative (evolutionary) game that can arise between the central bank and the private sector.⁴⁰

The general form of the central bank credibility game. We proceed by describing the credibility game between the central bank and private agents in general terms. The (evolutionary) game between the central bank and private agents consists of:

1. Two players referred as the central bank (cb) and the private sector (pa), i.e., $M = \{cb, pa\}$.
2. A strategy set S_i for each player $i \in M$ with two pure strategies which are to comply (C) or to deviate (D), i.e., $S_i = \{C, D\}$ for each $i \in M$.
3. A linear payoff function $u_i : S_i \rightarrow \mathbb{R}$, assigned to each player $i \in M$, which can be written in matrix form as $u_i(s_i) = Z_i s_i \in \mathbb{R}$ for any payoff matrix Z_i and strategy $s_i \in S_i$, for each player $i \in M$.

We define the strategy space of the game as $S = \prod_{i \in M} S_i$ where each strategy pair is pin down as $s = (s_{pa}, s_{cb}) \in S$. Denoting $s_i \in S_i$ the strategy of player $i \in M$ and the strategy of the other player as $s_{-i} := (s_j) \in S_{-i} = \prod_{j \in M, j \neq i} S_j$ where $j \neq i$ and $i, j \in M$, it follows that the strategy pair can be rewritten as $s := (s_i, s_{-i}) \in S_i \times S_{-i} = S = \prod_{i \in M} S_i$ for all $i \in M$.

⁴⁰In other words, there are payoffs (like in the well-known “game of chicken”) where a mixed strategy equilibrium exists and is evolutionarily stable which supports the notion that there is some degree of imperfect central bank credibility.

From here, we define a best response for a given player in the following general terms:

Definition 1 A strategy $\widehat{s}_i \in S_i$ is called a best response to strategy $s_{-i} \in S_{-i}$ iff $u_i(\widehat{s}_i, s_{-i}) \geq u_i(s_i, s_{-i})$, $\forall i \in M$, $\forall s_i \in S_i$.

If every player chooses its best response, then no other strategy can increase the player's payoff. Hence, all players following their best response strategies constitutes a Nash equilibrium defined as follows:

Definition 2 A pair of strategies $s^* \in S$ is called a Nash equilibrium iff $u_i(s^*) = u_i(s_i^*, s_{-i}^*) \geq u_i(s_i, s_{-i}^*)$, $\forall i \in M$, $\forall s_i \in S_i$.

A Nash equilibrium is a strategy pair in the game that is a best response for both players simultaneously so no player can benefit from switching to play another alternative strategy. In other words, if player $i \in M$ were to choose the alternative strategy $s_i \neq s_i^*$ where $s_i \in S_i$ instead of the strategy s_i^* receives a payoff $u_i(s_i, s_{-i}^*) \leq u_i(s_i^*, s_{-i}^*)$, i.e., s_i^* does just as good or better than any other alternative strategy. However, a Nash equilibrium allows for the possibility that some alternative strategy may achieve the same payoff, i.e., there may be some $s_i \in S_i$ for which $u_i(s_i, s_{-i}^*) = u_i(s_i^*, s_{-i}^*)$. In turn, an evolutionary stable strategy (ESS) is a strategy that supports a stable solution that has the stronger property that, if the strategy is followed, no player who adopts a novel strategy can hope to successfully displace the ESS strategy. More precisely, a ESS strategy can be defined in the following terms:

Definition 3 A strategy $s_i^{ESS} \in S_i$ for each $i \in M$ is an evolutionary stable strategy (ESS) if: either (a) $u_i(s_i^{ESS}, s_{-i}^{ESS}) > u_i(s_i, s_{-i}^{ESS})$, $\forall s_i \in S_i$ and $s_i \neq s_i^{ESS}$; or (b) $u_i(s_i^{ESS}, s_{-i}^{ESS}) = u_i(s_i, s_{-i}^{ESS})$ and $u_i(s_i^{ESS}, s_{-i}) > u_i(s_i, s_{-i})$, $\forall (s_i, s_{-i}) \in S$ and $s_i \neq s_i^{ESS}$ and $s_{-i} \neq s_{-i}^{ESS}$.

The ESS concept is an equilibrium refinement to the Nash equilibrium. What this means is that a strategy pair $(s_i^{ESS}, s_{-i}^{ESS})$ describes an ESS strategy for each player if: (a) the ESS strategy does strictly better than any alternative would do while playing against ESS; or (b) some alternative strategy does as well as ESS playing against ESS but ESS still does strictly better playing against the alternative strategy than it would do playing the alternative strategy against itself.

The linear payoff function $u_i : \{C, D\} \times \{C, D\} \rightarrow \mathbb{R}$ for both players (the central bank and the private sector) and two strategies (**C**omply or **D**eviate) can be described in normal

form with the following payoff matrix:

		Private Agents	
		C	D
Central Bank	C	R_{cb}, R_{pa}	L_{cb}, T_{pa}
	D	T_{cb}, L_{pa}	P_{cb}, P_{pa}

To comply (C) means to commit to honor the policy announcements on the part of the central bank and to accept the credibility of such commitments on the part of the private agents, while to deviate (D) means to renege on the policy announcements and to rely on a forecasting model not containing policy announcements (e.g., equation (25)) to negate any credibility to such announcements respectively.

We assume that the payoff for the private sector and the central bank is tied to the social welfare achieved. \mathbf{R} refers to the reward or social welfare that both players achieve jointly by each choosing C . If the two players deviate then each receives \mathbf{P} which is the punishment payoff (the sub-optimal social welfare) that they achieve jointly by each choosing D . In our context, the social welfare that can be achieved when both players deviate is lower than if both comply, i.e., $P > R$.

When one player complies and the other deviates, \mathbf{T} is the temptation payoff that the player that deviates (D) receives while \mathbf{L} is the loser payoff received by the player that complies (C). In our context, the player that deviates (or cheats) in this game benefits at the expense of the player that complies, i.e., the social welfare perceived by the player that is cheated is lower than that of the cheater such that $L_i < T_i, \forall i \in M$.

For expositional tractability, we assume that the temptation and loser payoffs are symmetric for both players, i.e., $L_i = L$ and $T_i = T, \forall i \in M$. Similarly, the reward and punishment values are also symmetric for both players, i.e., $R_i = R$ and $P_i = P, \forall i \in M$. Given the symmetric payoff matrix that we describe here, the linear payoff function can be written in matrix form as $u_i(s_i) = Z_i s_i \in \mathbb{R}$ for any strategy $s_i \in S_i$ and for each player $i \in M$ with $Z_i = Z = \begin{bmatrix} R & L \\ T & P \end{bmatrix}$.

Now, depending on the ordering of $R, T, L,$ and $P,$ we can have significantly different

games with different equilibrium outcomes. A well-known game, the Prisoner's Dilemma, requires the ordering to be $T > R > P > L$. We consider however two other orderings that stand out as most relevant for the interaction between the central bank and the private sector: the Game of Chicken which requires $T > R > L > P$ and the Trust Dilemma that requires instead that $R > T > L > P$.

Replicator dynamics. Let us consider $p_j(t)$ the frequency with which pure strategy $j = \{C, D\}$ is played and $p(t) = (p_C(t), p_D(t))^T$ the corresponding state vector, where t denotes the t -th replication of the same game. We postulate a law of motion for $p(t)$ that describes how the dynamics of the game evolve as players consider future generations (or replications) of the game at play. If players engage in a symmetric game with the payoff matrix Z , then $(Zp(t))_j$ is the expected payoff for strategy $j = \{C, D\}$ and $(p(t)^T Zp(t))$ is the average payoff. Thus, the relative performance of the frequency vector $p_j(t)$ for each strategy $j = \{C, D\}$ is given by $\frac{(Zp(t))_j}{p(t)^T Zp(t)}$ if $p(t)^T Zp(t) \neq 0$.

We assume that the frequency $p_j(t)$ for each strategy $j = \{C, D\}$ is iteratively updated proportionally to its relative performance, i.e.,

$$\frac{p_j(t + \Delta t)}{p_j(t)} = \frac{(Zp(t))_j}{p(t)^T Zp(t)} \Delta t, \quad (35)$$

for $\Delta t > 0$ and for all $j = \{C, D\}$. Hence, $p_j(t + \Delta t) - p_j(t) = p_j(t) \frac{(Zp(t))_j - p(t)^T Zp(t)}{p(t)^T Zp(t)} \Delta t$. This, in turn, yields the following differential equation as $\Delta t \rightarrow 0$:

$$\dot{p}_j = p_j \frac{(Zp)_j - p^T Zp}{p^T Zp}, \quad (36)$$

for all $j = \{C, D\}$ with \dot{p}_j denoting the derivative of $p_j(t)$ with respect to t .

A solution $q_j(t)$ to the simplified differential equation:

$$\dot{q}_j = q_j \left[(Zq)_j - q^T Zq \right], \quad (37)$$

suffices to describe the replicator dynamics of the game as (36) has the same trajectories as (37). That is because, according to the transformation of t given by $t(s) = \int_{s_0}^s p(t)^T Zp(t)$ with s_0 being the initial iteration, every solution $p_j(t)$ of (36) delivers a solution $q_j(s) := p_j(t(s))$ of the simplified differential equation (37).

Evolutionary stable strategies. Let us denote the frequency of strategy D with the parameter q and the frequency of strategy C as $1 - q$ with $\tilde{q} = (1 - q, q)^T$. The replicator equation in (37) has two terms that depend on the payoff matrix Z . The first term depends on $Z\tilde{q}$ which gives us that $\begin{pmatrix} (1 - q)R + qL \\ (1 - q)T + qP \end{pmatrix}$. Since strategy D is ordered after C in the layout of the normal form of the game, we use the second component of $Z\tilde{q}$ to describe $(Z\tilde{q})_j$ when $j = D$. The second term $\tilde{q}^T Z\tilde{q}$ can be expressed as $(1 - q)^2 R + (1 - q)q(L + T) + q^2 P$. Thus, the replicator equation in (37) for strategy D is given by:

$$\dot{q} = q [(1 - q)T + qP - (1 - q)^2 R - (1 - q)q(L + T) - q^2 P]. \quad (38)$$

By setting $\dot{q} = 0$, i.e., by solving the equation:

$$q [T - R - (L - P + 2(T - R))q + (L - P + T - R)q^2] = 0, \quad (39)$$

we obtain the evolutionary states of the model. This holds trivially true for $q^{ES} = 0$ and for $q^{ES} = 1$. The mixed strategy solution can be pin down by factoring the roots from the quadratic function $q^2 - \left(\frac{L - P + 2(T - R)}{L - P + T - R}\right)q + \left(\frac{T - R}{L - P + T - R}\right) = 0$ where we already know that one of the roots is $q^{ES} = 1$. From that, we obtain that that the mixed strategy state of the model is $q^{ES} = \left(\frac{1}{1 + \frac{L - P}{T - R}}\right)$.

To sum up:

Lemma 1 *The central bank credibility game has generically three states. Two states are in pure strategies where $q^{ES} = 0$ implies playing C and $q^{ES} = 1$ implies playing D . The mixed strategy state, if one exists, involves playing strategy D with a frequency of $q^{ES} = \left(\frac{1}{1 + \frac{L - P}{T - R}}\right)$ and strategy C with a frequency of $1 - q^{ES} = \left(\frac{\frac{L - P}{T - R}}{1 + \frac{L - P}{T - R}}\right)$.*

The mixed strategy state is well-defined and satisfies $0 \leq \left(\frac{1}{1 + \frac{L - P}{T - R}}\right) \leq 1$ whenever $(L - P) + (T - R) \geq 0$ and $\frac{L - P}{T - R} \geq 0$. The Prisoner's Dilemma, as indicated before, requires the ordering to be $T > R > P > L$. Therefore, $T - R > 0$ and $L - P < 0$ violates the condition that $\frac{L - P}{T - R} \geq 0$ and for this case there are only two states based on pure strategies. Similarly, the Trust Dilemma that imposes instead that $R > T > L > P$ implies that $L - P > 0$ and $T - R < 0$. Therefore, for the Trust Dilemma, there are only two states in pure strategies as well. In turn, the Game of Chicken which requires $T > R > L > P$

implies that $L - P > 0$ and $T - R > 0$ and satisfies the conditions that insure a well-defined mixed strategy state exists.

Definition 4 A strategy pair $(1 - q^{ESS}, q^{ESS})^T$ is said to be an evolutionary stable strategy (ESS) if it's a locally convergent evolutionary state which is dynamically restored after a disturbance via the replicator equation in (37), provided the disturbance is not too large. That is, $q^{ES} = 0$ is an ESS if $\dot{q} < 0$ for $q^0 (> 0) \rightarrow 0$ from the right and $q^{ES} = 1$ is an ESS if $\dot{q} > 0$ for $q^0 (< 1) \rightarrow 1$ from the left. In turn, $q^{ES} = \left(\frac{1}{1 + \frac{L-P}{T-R}}\right)$ is an ESS if $\dot{q} < 0$ for $q^0 \left(> \frac{1}{1 + \frac{L-P}{T-R}}\right) \rightarrow \frac{1}{1 + \frac{L-P}{T-R}}$ from the right and $\dot{q} > 0$ for $q^0 \left(< \frac{1}{1 + \frac{L-P}{T-R}}\right) \rightarrow \frac{1}{1 + \frac{L-P}{T-R}}$ from the left.

When we explore the dynamics implied by the replicator equation in (37), it follows that given the orderings of the payoffs $R, T, L,$ and P :

Proposition 1 The Prisoner's Dilemma game has one ESS only, that is the state $q^{ESS} = q^{ES} = 1$ (which implies the player follows the pure strategy D). Similarly, the Trust Dilemma has one ESS only that corresponds to the other pure strategy $q^{ESS} = q^{ES} = 0$ (the player follows the pure strategy C). In turn, the only ESS of the central bank credibility game (the Game of Chicken between the central bank and the private sector) is the mixed strategy implied by $q^{ESS} = q^{ES} = \left(\frac{1}{1 + \frac{L-P}{T-R}}\right)$.

When we estimate our model with central bank credibility and forward guidance in Section 4, the data favor a mixed strategy equilibrium. Thus, Proposition 1 suggests that the Game of Chicken is better suited than the Prisoner's Dilemma or the Trust Dilemma to describe the central bank credibility game. In other words, the Game of Chicken where a mixed strategy equilibrium exists and is evolutionarily stable can support the notion that there is some degree of imperfect central bank credibility that we detect in the U.S. data.

We leave for future research the tasks of relaxing the symmetry of the payoff matrix used here for exposition and of incorporating those payoffs and dynamic learning via the replicator dynamics in our model estimation. That would help us endogenize the equilibrium credibility parameter and introduce learning in our framework.

8. Tables

Table 1: Prior & Posterior Estimates of Structural Parameters

Prior Distr.		Posterior Distribution					
		Perfectly Credible C.B. ($\tau = 1$)			Not Perfectly Credible C.B. ($\hat{\tau}$)		
	Distr.	Mean	5%	95%	Mean	5%	95%
τ	B(0.80, 0.01)	-	-	-	0.77	0.75	0.79
ω	N(1.00, 0.05)	0.97	0.89	1.05	1.00	0.91	1.08
ρ	B(0.75, 0.10)	0.88	0.86	0.90	0.97	0.95	0.98
χ_π	N(1.50, 0.10)	1.33	1.18	1.47	1.50	1.33	1.66
χ_x	N(0.125, 0.05)	0.07	0.04	0.10	0.13	0.05	0.21
ι_p	B(0.50, 0.15)	0.07	0.02	0.11	0.68	0.54	0.82
ρ_γ	B(0.50, 0.20)	0.99	0.99	0.995	0.50	0.48	0.52
ρ_μ	B(0.50, 0.20)	0.50	0.43	0.58	0.03	0.00	0.05
σ_γ	IG(0.30, 2.00)	0.08	0.06	0.09	0.60	0.54	0.66
σ_μ	IG(0.30, 2.00)	0.11	0.09	0.12	0.13	0.12	0.15
σ_{MP}	IG(0.30, 2.00)	0.19	0.17	0.20	0.19	0.17	0.21
σ_1^{FG}	IG(0.30, 2.00)	0.07	0.06	0.09	0.07	0.06	0.08
σ_2^{FG}	IG(0.30, 2.00)	0.04	0.04	0.04	0.05	0.04	0.06
σ_3^{FG}	IG(0.30, 2.00)	0.04	0.04	0.04	0.04	0.04	0.05
σ_4^{FG}	IG(0.30, 2.00)	0.04	0.04	0.04	0.04	0.04	0.05
σ_5^{FG}	IG(0.30, 2.00)	0.06	0.05	0.07	0.06	0.05	0.07
σ_6^{FG}	IG(0.30, 2.00)	0.06	0.05	0.07	0.06	0.05	0.07
σ_7^{FG}	IG(0.30, 2.00)	0.06	0.05	0.07	0.06	0.05	0.07
σ_8^{FG}	IG(0.30, 2.00)	0.06	0.05	0.07	0.06	0.05	0.07
σ_9^{FG}	IG(0.30, 2.00)	0.06	0.05	0.07	0.06	0.05	0.07
σ_{10}^{FG}	IG(0.30, 2.00)	0.06	0.05	0.07	0.06	0.05	0.07
σ_{11}^{FG}	IG(0.30, 2.00)	0.06	0.05	0.07	0.06	0.05	0.07
σ_{12}^{FG}	IG(0.30, 2.00)	0.06	0.05	0.07	0.06	0.05	0.07
	logMargL	599.08			901.18		

Note: C.B.: Central Bank, G: Gamma Distribution, N: Normal Distribution, B: Beta Distribution, U: Uniform Distribution, IG: Inverse-Gamma Distribution.

Table 2: **Prior & Posterior Estimates of Measurement Errors**

Prior Distr.		Posterior Distribution					
		Perfectly Credible C.B. ($\tau = 1$)			Not Perfectly Credible C.B. ($\hat{\tau}$)		
	Distr.	Mean	5%	95%	Mean	5%	95%
$\sigma_{g^1}^{me}$	IG(0.10, 2.00)	0.45	0.41	0.49	0.34	0.31	0.38
$\sigma_{g^2}^{me}$	IG(0.10, 2.00)	0.45	0.40	0.50	0.19	0.17	0.21
$\sigma_{\pi^1}^{me}$	IG(0.10, 2.00)	0.17	0.15	0.18	0.16	0.15	0.18
$\sigma_{i^1}^{me}$	IG(0.10, 2.00)	0.03	0.03	0.04	0.03	0.02	0.03
$\sigma_{i^2}^{me}$	IG(0.10, 2.00)	0.02	0.01	0.02	0.02	0.01	0.02
$\sigma_{i^3}^{me}$	IG(0.10, 2.00)	0.02	0.01	0.02	0.01	0.01	0.02
$\sigma_{i^4}^{me}$	IG(0.10, 2.00)	0.02	0.01	0.02	0.02	0.01	0.02
$\sigma_{i^5}^{me}$	IG(0.10, 2.00)	0.02	0.02	0.03	0.02	0.02	0.03
logMargL		599.08			901.18		

Note: C.B.: Central Bank, G: Gamma Distribution, N: Normal Distribution, B: Beta Distribution, U: Uniform Distribution, IG: Inverse-Gamma Distribution.

Table 3: Variance Decomposition Upon Impact

	Perfectly Credible C.B. ($\tau = 1$)			Not Perfectly Credible C.B. ($\hat{\tau}$)		
	Output	Inflation	Interest Rate	Output	Inflation	Interest Rate
ε_t^{MP}	30.33	0.50	95.54	83.22	0.00	99.67
ε_t^γ	44.70	12.73	0.99	0.01	0.00	0.00
ε_t^μ	1.83	85.41	3.29	9.23	99.99	0.32
$\varepsilon_{1,t}^{FG}$	5.20	0.10	0.02	6.38	0.00	0.00
$\varepsilon_{2,t}^{FG}$	1.47	0.03	0.01	1.02	0.00	0.00
$\varepsilon_{3,t}^{FG}$	1.27	0.04	0.01	0.12	0.00	0.00
$\varepsilon_{4,t}^{FG}$	1.25	0.05	0.01	0.01	0.00	0.00
$\varepsilon_{5,t}^{FG}$	2.61	0.12	0.02	0.00	0.00	0.00
$\varepsilon_{6,t}^{FG}$	2.24	0.12	0.02	0.01	0.00	0.00
$\varepsilon_{7,t}^{FG}$	1.94	0.13	0.02	0.00	0.00	0.00
$\varepsilon_{8,t}^{FG}$	1.74	0.14	0.02	0.00	0.00	0.00
$\varepsilon_{9,t}^{FG}$	1.55	0.14	0.02	0.00	0.00	0.00
$\varepsilon_{10,t}^{FG}$	1.40	0.15	0.02	0.00	0.00	0.00
$\varepsilon_{11,t}^{FG}$	1.28	0.16	0.02	0.00	0.00	0.00
$\varepsilon_{12,t}^{FG}$	1.17	0.17	0.02	0.00	0.00	0.00
Total FG	23.14	1.36	0.21	7.54	0.00	0.00

Note: This table computes the conditional variance decomposition upon impact of the structural and forward guidance shocks with parameter values at their posterior mean. Each column displays the percentage contribution of each shock to model-implied output and observables (inflation and interest rates). Total FG denotes the sum of all of the forward guidance shocks. The measurement errors are not shown as their contribution concerns expected values of observables.

Table 4: **Posterior Estimates of Structural Parameters Without Frictions**

Prior Distr.		Posterior Distribution					
		No Habits ($\eta = 0$)			No Price Indexation ($\iota_p = 0$)		
	Distr.	Mean	5%	95%	Mean	5%	95%
τ	B(0.80, 0.01)	0.76	0.75	0.78	0.78	0.76	0.80
	logMargL	635.97			890.70		

Note: B: Beta Distribution.

Table 5: **Estimated Elasticity of Output with Respect to 1-Year Ahead Expected Interest Rates**

	Perfectly Credible C.B. ($\tau = 1$)	Not Perfectly Credible C.B. ($\hat{\tau}$)
Elasticity of y w.r.t. $\mathbb{E}_t^{obs}(i_{t+4})$	-5.28	-0.65
Elasticity of π_t^{obs} w.r.t. $\mathbb{E}_t^{obs}(i_{t+4})$	-0.10	-0.03

Table 6: **Prior & Posterior Estimates of Structural Parameters with Alternative Non-Credible Expectations**

Prior Distr.		Posterior Distribution		
	Distr.	Mean	5%	95%
τ	B(0.80, 0.01)	0.78	0.76	0.79
ω	N(1.00, 0.05)	1.00	0.91	1.08
ρ	B(0.75, 0.10)	0.98	0.97	0.99
χ_π	N(1.50, 0.10)	1.49	1.33	1.66
χ_x	N(0.125, 0.05)	0.13	0.05	0.21
ι_p	B(0.50, 0.15)	0.71	0.58	0.85
ρ_γ	B(0.50, 0.20)	0.47	0.43	0.50
ρ_μ	B(0.50, 0.20)	0.03	0.00	0.06
σ_γ	IG(0.30, 2.00)	0.60	0.54	0.66
σ_μ	IG(0.30, 2.00)	0.14	0.12	0.16
σ_{MP}	IG(0.30, 2.00)	0.19	0.17	0.21
σ_1^{FG}	IG(0.30, 2.00)	0.07	0.06	0.08
σ_2^{FG}	IG(0.30, 2.00)	0.04	0.04	0.05
σ_3^{FG}	IG(0.30, 2.00)	0.04	0.04	0.04
σ_4^{FG}	IG(0.30, 2.00)	0.04	0.04	0.04
σ_5^{FG}	IG(0.30, 2.00)	0.06	0.05	0.07
σ_6^{FG}	IG(0.30, 2.00)	0.06	0.05	0.07
σ_7^{FG}	IG(0.30, 2.00)	0.06	0.05	0.07
σ_8^{FG}	IG(0.30, 2.00)	0.06	0.05	0.07
σ_9^{FG}	IG(0.30, 2.00)	0.06	0.05	0.07
σ_{10}^{FG}	IG(0.30, 2.00)	0.06	0.05	0.07
σ_{11}^{FG}	IG(0.30, 2.00)	0.06	0.05	0.07
σ_{12}^{FG}	IG(0.30, 2.00)	0.06	0.05	0.07
logMargL		928.88		

Note: G: Gamma Distribution, N: Normal Distribution, B: Beta Distribution, U: Uniform Distribution, IG: Inverse-Gamma Distribution.

Table 7: **Prior & Posterior Estimates of Measurement Errors with Alternative Non-Credible Expectations**

Prior Distr.		Posterior Distribution		
Distr.		Mean	5%	95%
$\sigma_{g^1}^{me}$	IG(0.10, 2.00)	0.34	0.31	0.37
$\sigma_{g^2}^{me}$	IG(0.10, 2.00)	0.19	0.17	0.21
$\sigma_{\pi^1}^{me}$	IG(0.10, 2.00)	0.16	0.14	0.17
$\sigma_{i^1}^{me}$	IG(0.10, 2.00)	0.02	0.02	0.02
$\sigma_{i^2}^{me}$	IG(0.10, 2.00)	0.02	0.01	0.02
$\sigma_{i^3}^{me}$	IG(0.10, 2.00)	0.01	0.01	0.02
$\sigma_{i^4}^{me}$	IG(0.10, 2.00)	0.02	0.01	0.02
$\sigma_{i^5}^{me}$	IG(0.10, 2.00)	0.02	0.02	0.02
logMargL		928.88		

Note: G: Gamma Distribution, N: Normal Distribution, B: Beta Distribution, U: Uniform Distribution, IG: Inverse-Gamma Distribution.

Table 8: Prior & Posterior Estimates of Structural Parameters under Robustness Checks

Prior Distr.		Posterior Distribution											
		Non-ZLB			Great Moderation			U(0,1) Prior on τ			Alternative SPF Timing		
	Distr.	Mean	5%	95%	Mean	5%	95%	Mean	5%	95%	Mean	5%	95%
τ	B(0.80, 0.01)	0.78	0.76	0.79	0.78	0.76	0.80	0.60	0.57	0.64	0.78	0.76	0.79
ω	N(1.00, 0.05)	1.00	0.91	1.08	1.00	0.92	1.08	1.00	0.91	1.08	0.99	0.91	1.08
ρ	B(0.75, 0.10)	0.95	0.94	0.97	0.95	0.93	0.98	0.98	0.96	0.99	0.95	0.94	0.97
χ_π	N(1.50, 0.10)	1.49	1.33	1.65	1.50	1.34	1.66	1.52	1.36	1.68	1.49	1.33	1.65
χ_x	N(0.125, 0.05)	0.14	0.05	0.22	0.13	0.05	0.21	0.13	0.04	0.21	0.14	0.06	0.22
ι_p	B(0.50, 0.15)	0.65	0.51	0.80	0.40	0.23	0.58	0.58	0.39	0.78	0.68	0.54	0.82
ρ_γ	B(0.50, 0.20)	0.49	0.47	0.52	0.42	0.35	0.49	0.49	0.48	0.51	0.38	0.32	0.44
ρ_μ	B(0.50, 0.20)	0.04	0.00	0.07	0.08	0.01	0.15	0.04	0.00	0.07	0.03	0.00	0.06
σ_γ	IG(0.30, 2.00)	0.65	0.57	0.72	0.55	0.47	0.64	0.60	0.54	0.66	0.70	0.62	0.79
σ_μ	IG(0.30, 2.00)	0.13	0.11	0.15	0.12	0.11	0.14	0.14	0.13	0.16	0.14	0.12	0.15
σ_{MP}	IG(0.30, 2.00)	0.22	0.19	0.24	0.14	0.13	0.16	0.20	0.18	0.23	0.19	0.17	0.21
σ_1^{FG}	IG(0.30, 2.00)	0.08	0.06	0.09	0.06	0.05	0.08	0.08	0.07	0.10	0.09	0.08	0.10
σ_2^{FG}	IG(0.30, 2.00)	0.06	0.05	0.06	0.06	0.05	0.07	0.06	0.05	0.07	0.04	0.04	0.05
σ_3^{FG}	IG(0.30, 2.00)	0.05	0.04	0.05	0.04	0.04	0.05	0.05	0.04	0.06	0.04	0.04	0.05
σ_4^{FG}	IG(0.30, 2.00)	0.05	0.04	0.05	0.04	0.04	0.05	0.05	0.04	0.06	0.06	0.05	0.08
σ_5^{FG}	IG(0.30, 2.00)	0.07	0.05	0.08	0.07	0.05	0.09	0.06	0.05	0.07	0.06	0.05	0.08
σ_6^{FG}	IG(0.30, 2.00)	0.07	0.05	0.08	0.07	0.05	0.09	0.06	0.05	0.07	0.06	0.05	0.08
σ_7^{FG}	IG(0.30, 2.00)	0.06	0.05	0.08	0.07	0.05	0.09	0.06	0.05	0.07	0.06	0.05	0.08
σ_8^{FG}	IG(0.30, 2.00)	0.07	0.05	0.08	0.07	0.05	0.09	0.06	0.05	0.07	0.06	0.05	0.08
σ_9^{FG}	IG(0.30, 2.00)	0.07	0.05	0.08	0.07	0.05	0.09	0.06	0.05	0.07	0.06	0.05	0.07
σ_{10}^{FG}	IG(0.30, 2.00)	0.07	0.05	0.08	0.07	0.05	0.09	0.06	0.05	0.07	0.06	0.05	0.08
σ_{11}^{FG}	IG(0.30, 2.00)	0.07	0.05	0.08	0.07	0.05	0.09	0.06	0.05	0.07	0.06	0.05	0.08
σ_{12}^{FG}	IG(0.30, 2.00)	0.07	0.05	0.08	0.07	0.05	0.09	0.06	0.05	0.00	0.06	0.05	0.08
logMargL		587.74			601.75			928.46			631.36		

Note: G: Gamma Distribution, N: Normal Distribution, B: Beta Distribution, U: Uniform Distribution, IG: Inverse-Gamma Distribution.

Table 9: **Prior & Posterior Estimates of Measurement Errors under Robustness Checks**

Prior Distr.		Posterior Distribution											
		Non-ZLB			Great Moderation			U(0,1) Prior on τ			Alternative SPF Timing		
Distr.		Mean	5%	95%	Mean	5%	95%	Mean	5%	95%	Mean	5%	95%
$\sigma_{g^1}^{me}$	IG(0.10, 2.00)	0.33	0.30	0.37	0.29	0.25	0.32	0.34	0.31	0.37	0.32	0.29	0.35
$\sigma_{g^2}^{me}$	IG(0.10, 2.00)	0.20	0.18	0.22	0.18	0.15	0.20	0.19	0.17	0.21	0.19	0.17	0.21
$\sigma_{\pi^1}^{me}$	IG(0.10, 2.00)	0.17	0.15	0.19	0.17	0.15	0.19	0.15	0.14	0.17	0.18	0.16	0.20
$\sigma_{i^1}^{me}$	IG(0.10, 2.00)	0.03	0.03	0.04	0.04	0.03	0.04	0.03	0.02	0.03	0.02	0.02	0.02
$\sigma_{i^2}^{me}$	IG(0.10, 2.00)	0.02	0.02	0.02	0.02	0.01	0.02	0.02	0.01	0.02	0.02	0.01	0.02
$\sigma_{i^3}^{me}$	IG(0.10, 2.00)	0.02	0.01	0.02	0.02	0.01	0.02	0.01	0.01	0.02	0.02	0.01	0.02
$\sigma_{i^4}^{me}$	IG(0.10, 2.00)	0.02	0.01	0.02	0.02	0.01	0.02	0.02	0.01	0.02	0.02	0.02	0.02
$\sigma_{i^5}^{me}$	IG(0.10, 2.00)	0.02	0.02	0.03	0.02	0.02	0.03	0.02	0.02	0.03	-	-	-
logMargL		587.74			601.75			928.46			631.36		

Note: G: Gamma Distribution, N: Normal Distribution, B: Beta Distribution, U: Uniform Distribution, IG: Inverse-Gamma Distribution.

9. Figures

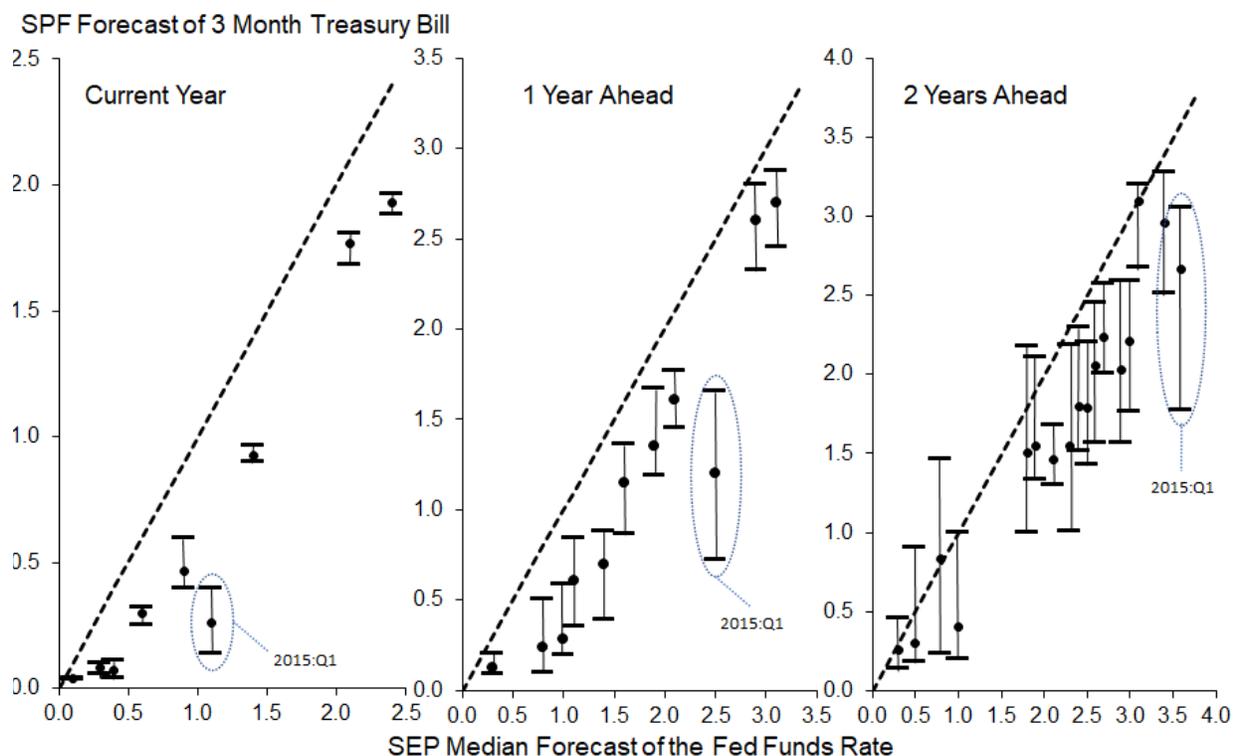


Figure 1: Range of Pooled 3-Month Interest Rate Projections from Survey of Professional Forecasters (SPF) vs. Federal Reserve’s median Summary of Economic Projections (SEP) on the Fed Funds Rate

Note: Bars represent the 75th and 25th percentile while the dot indicates the median (50th percentile) of the pooled individual SPF forecasts conditional on each given value of the SEP median forecast over the sample period. Data covers from 2012:Q1 till 2018:Q4. The dashed line plots the 45 degree line for reference. 2015:Q1 is the most significant outlier between the policy path indicated in the SEP and the SPF forecasts. This occurred as the Fed’s language shifted to prepare markets for liftoff from the ZLB. SOURCES: Federal Reserve’s Summary of Economic Projections (SEP); Survey of Professional Forecasters (SPF); authors’ calculations.

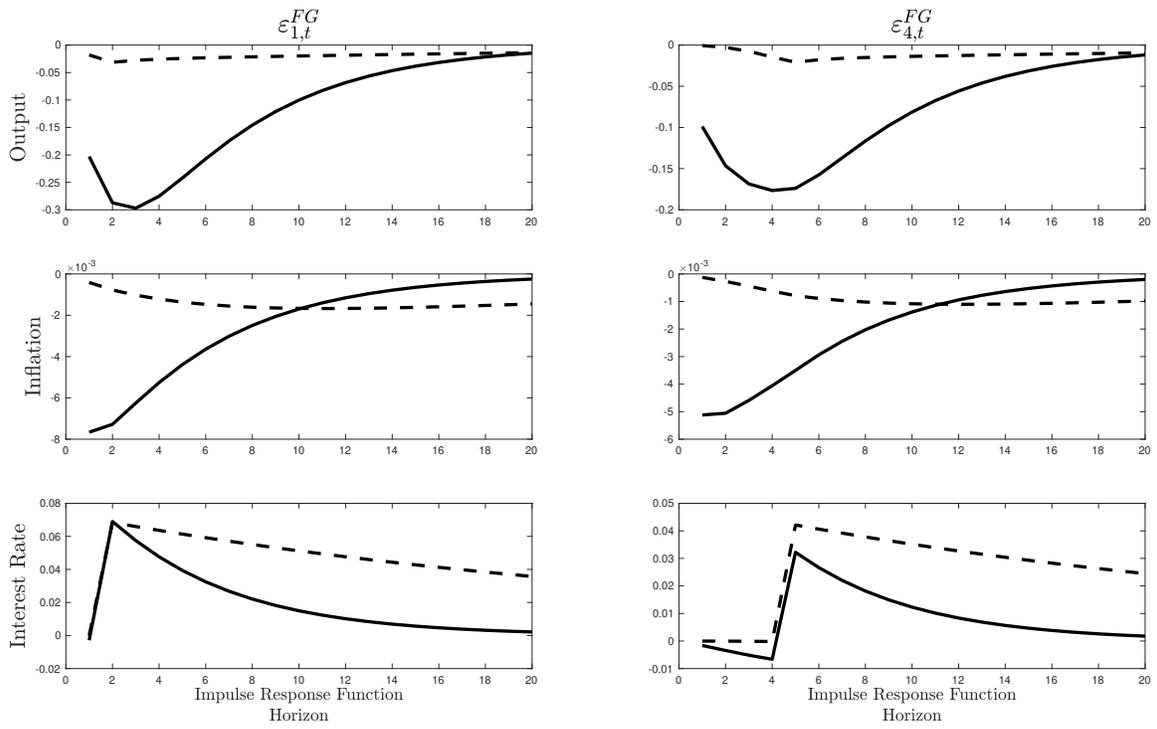


Figure 2: Impulse Response Functions. Mean response of model-implied output and observables (inflation and interest rate) to *one-period ahead forward guidance* and *four-period ahead forward guidance* shocks. Solid Line: Perfectly Credible C.B. (i.e., $\tau = 1$). Dashed line: Not Perfectly Credible C.B. (i.e., Benchmark $\hat{\tau}$). C.B.: Central Bank.

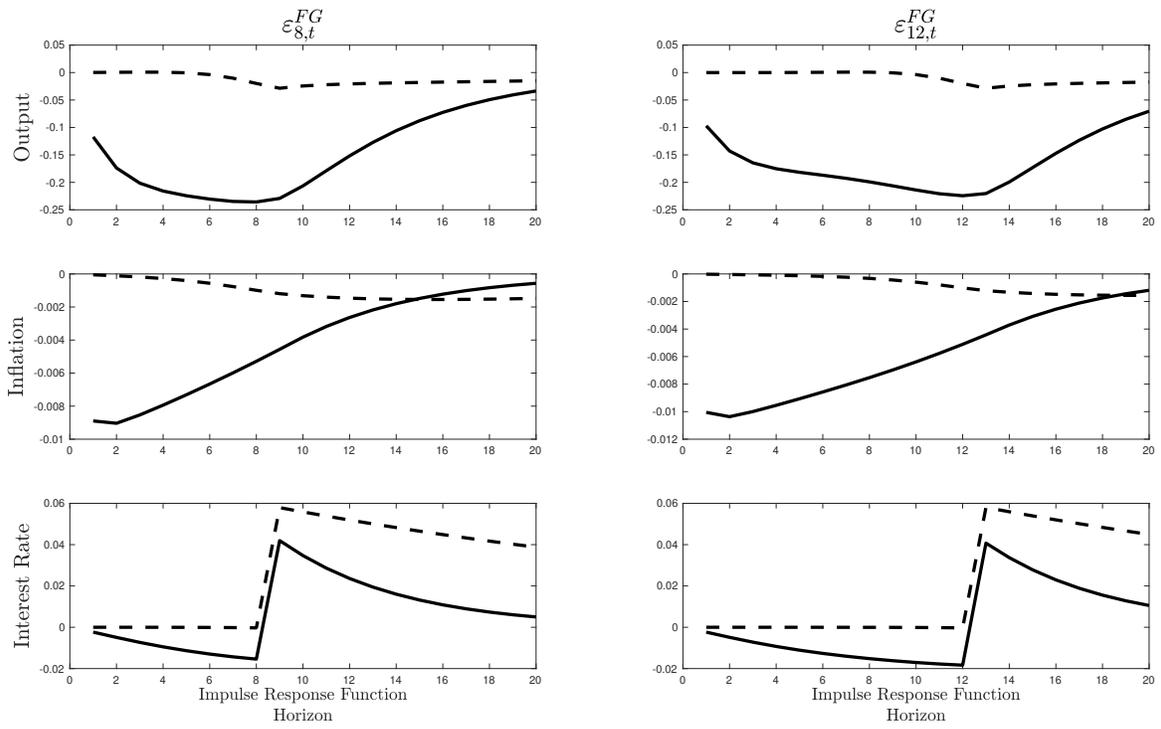


Figure 3: Impulse Response Functions. Mean response of model-implied output and observables (inflation and interest rate) to *eight-period ahead forward guidance* and *twelve-period ahead forward guidance* shocks. Solid Line: Perfectly Credible C.B. (i.e., $\tau = 1$). Dashed line: Not Perfectly Credible C.B. (i.e., Benchmark $\hat{\tau}$). C.B.: Central Bank.

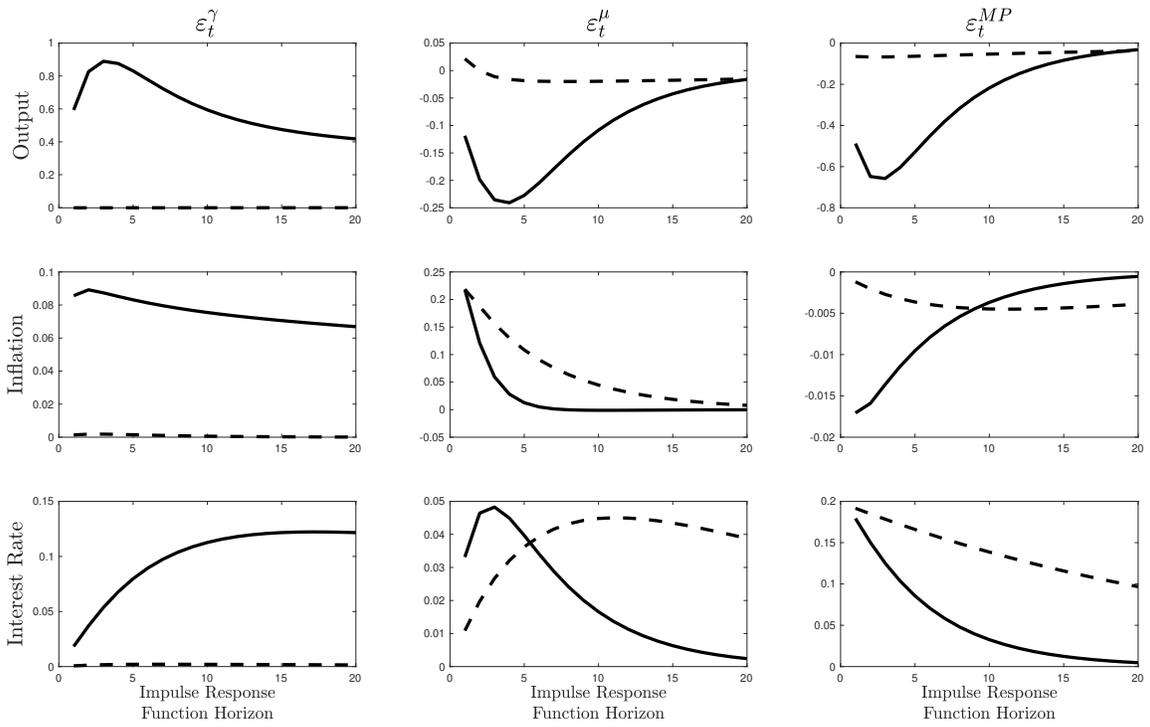


Figure 4: Impulse Response Functions. Mean response of model-implied output and observables (inflation and interest rate) to *productivity growth*, *cost-push*, and *unanticipated monetary policy* shocks. Solid Line: Perfectly Credible C.B. (i.e., $\tau = 1$). Dashed line: Not Perfectly Credible C.B. (i.e., Benchmark $\hat{\tau}$). C.B.: Central Bank.

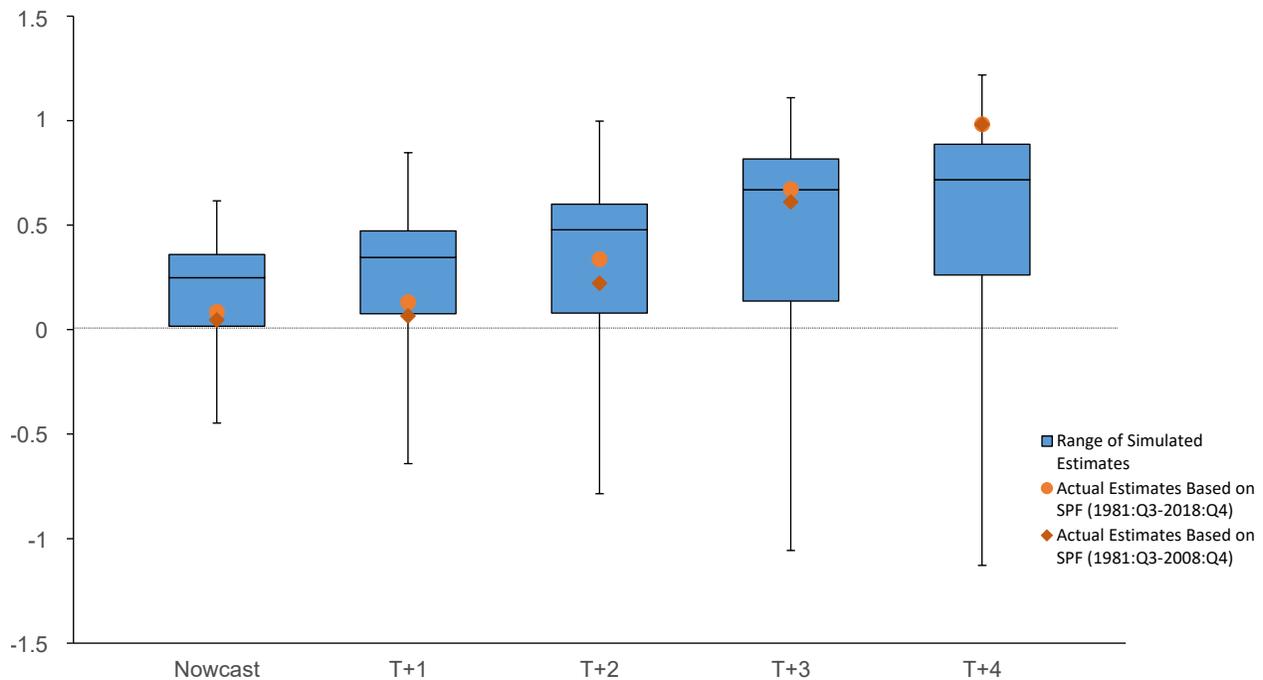


Figure 5: Estimates of Forecasting Errors Response to Forecasting Disagreement, Survey of Professional Forecasters (SPF) vs. Simulated Data

Note: Forecasting errors are computed with respect to the mean forecast with SPF data from 1981:Q3 until 2018:Q4 (150 observations). Forecasting disagreements are measured with the interquartile range of the cross-sectional distribution of individual forecasts in order to make the empirical results less sensitive to outliers. We regress forecasting errors on an intercept and this measure of forecasting disagreement for all available time horizons. We perform the same exercise on a rolling window of 150 observations from a simulated sample data of 2000 observations under $\hat{\tau}$. We represent the full range of rolling window estimates with a box-and-whisker plot that show their min, max, median, and interquartile range. SOURCES: Survey of Professional Forecasters (SPF), simulated data, authors' calculations.

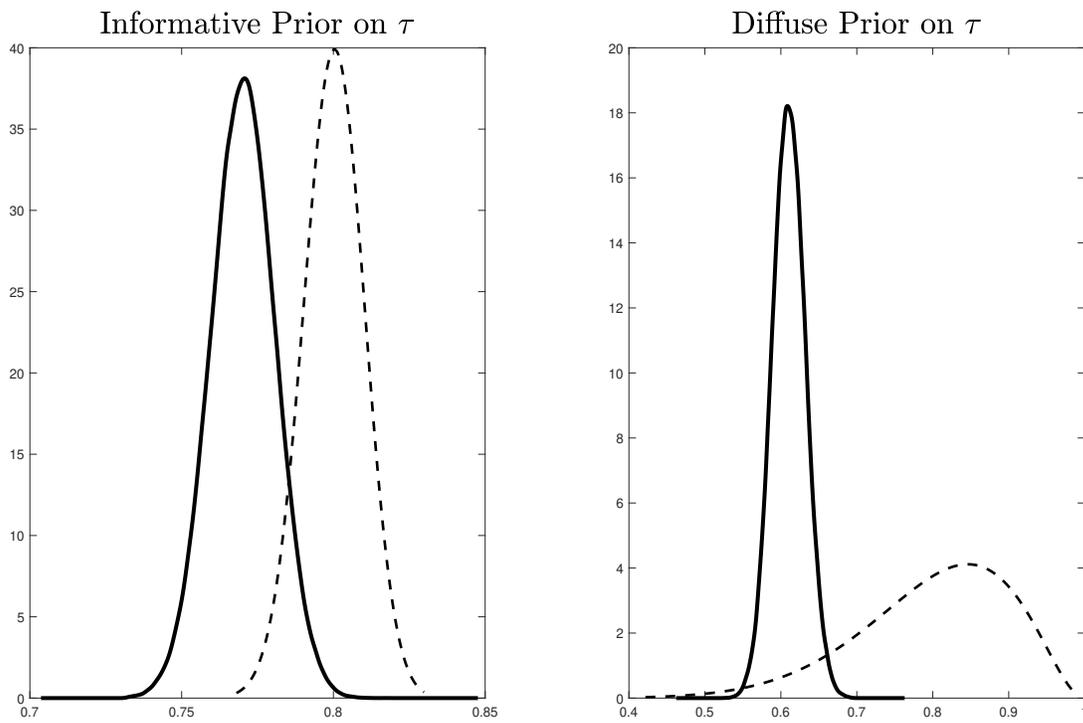


Figure 6: Posterior and Prior Distributions under Alternative Priors on τ . Left Panel: $B(0.80, 0.01)$ Prior, Right Panel: $B(0.80, 0.1)$ Prior. Solid Line: Posterior Distribution, Dashed Line: Prior Distribution

10. Online Appendix

Table 10: **Prior & Posterior Estimates of Structural Parameters Without Frictions**

Prior Distr.		Posterior Distribution					
		No Habits ($\eta = 0$)			No Price Indexation ($\iota_p = 0$)		
	Distr.	Mean	5%	95%	Mean	5%	95%
τ	B(0.80, 0.01)	0.76	0.75	0.78	0.78	0.76	0.80
ω	N(1.00, 0.05)	0.99	0.91	1.07	1.00	0.92	1.08
ρ	B(0.75, 0.10)	0.96	0.95	0.98	0.97	0.95	0.98
χ_π	N(1.50, 0.10)	1.50	1.33	1.66	1.50	1.34	1.66
χ_x	N(0.125, 0.05)	0.14	0.06	0.23	0.13	0.05	0.21
ι_p	B(0.50, 0.15)	0.68	0.55	0.81	-	-	-
ρ_γ	B(0.50, 0.20)	0.13	0.05	0.20	0.50	0.47	0.52
ρ_μ	B(0.50, 0.20)	0.03	0.00	0.05	0.75	0.65	0.85
σ_γ	IG(0.30, 2.00)	0.70	0.61	0.80	0.60	0.54	0.66
σ_μ	IG(0.30, 2.00)	0.14	0.12	0.15	0.08	0.06	0.09
σ_{MP}	IG(0.30, 2.00)	0.19	0.17	0.21	0.19	0.17	0.21
σ_1^{FG}	IG(0.30, 2.00)	0.07	0.06	0.08	0.07	0.06	0.08
σ_2^{FG}	IG(0.30, 2.00)	0.05	0.04	0.06	0.05	0.04	0.06
σ_3^{FG}	IG(0.30, 2.00)	0.04	0.04	0.05	0.04	0.04	0.04
σ_4^{FG}	IG(0.30, 2.00)	0.04	0.04	0.05	0.04	0.04	0.05
σ_5^{FG}	IG(0.30, 2.00)	0.06	0.05	0.07	0.06	0.05	0.07
σ_6^{FG}	IG(0.30, 2.00)	0.06	0.05	0.07	0.06	0.05	0.07
σ_7^{FG}	IG(0.30, 2.00)	0.06	0.05	0.07	0.06	0.05	0.07
σ_8^{FG}	IG(0.30, 2.00)	0.06	0.05	0.07	0.06	0.05	0.07
σ_9^{FG}	IG(0.30, 2.00)	0.06	0.05	0.07	0.06	0.05	0.07
σ_{10}^{FG}	IG(0.30, 2.00)	0.06	0.05	0.07	0.06	0.05	0.07
σ_{11}^{FG}	IG(0.30, 2.00)	0.06	0.05	0.07	0.06	0.05	0.07
σ_{12}^{FG}	IG(0.30, 2.00)	0.06	0.05	0.07	0.06	0.05	0.07
	logMargL	635.97			890.70		

Note: G: Gamma Distribution, N: Normal Distribution, B: Beta Distribution, U: Uniform Distribution, IG: Inverse-Gamma Distribution.

Table 11: **Prior & Posterior Estimates of Measurement Errors Without Frictions**

Prior Distr.		Posterior Distribution					
		No Habits ($\eta = 0$)			No Price Indexation ($\iota_p = 0$)		
	Distr.	Mean	5%	95%	Mean	5%	95%
$\sigma_{g^1}^{me}$	IG(0.10, 2.00)	0.85	0.77	0.93	0.35	0.31	0.38
$\sigma_{g^2}^{me}$	IG(0.10, 2.00)	0.26	0.23	0.29	0.19	0.17	0.21
$\sigma_{\pi^1}^{me}$	IG(0.10, 2.00)	0.17	0.15	0.18	0.18	0.16	0.19
$\sigma_{i^1}^{me}$	IG(0.10, 2.00)	0.03	0.02	0.04	0.03	0.02	0.04
$\sigma_{i^2}^{me}$	IG(0.10, 2.00)	0.02	0.01	0.02	0.02	0.01	0.02
$\sigma_{i^3}^{me}$	IG(0.10, 2.00)	0.02	0.01	0.02	0.01	0.01	0.02
$\sigma_{i^4}^{me}$	IG(0.10, 2.00)	0.02	0.01	0.02	0.02	0.01	0.02
$\sigma_{i^5}^{me}$	IG(0.10, 2.00)	0.02	0.02	0.03	0.02	0.02	0.03
logMargL		635.97			890.70		

Note: G: Gamma Distribution, N: Normal Distribution, B: Beta Distribution, U: Uniform Distribution, IG: Inverse-Gamma Distribution.